

# Wintertime Fjord-Shelf Interaction and Ice Sheet Melting in Southeast Greenland

Neil J. Fraser<sup>1,2</sup>, Mark E. Inall<sup>1,2</sup>, Marcello G. Magaldi<sup>3,4</sup>, Thomas W. N. Haine<sup>3</sup>, Sam C. Jones<sup>1</sup>

<sup>1</sup>The Scottish Association for Marine Science (SAMS), Scottish Marine Institute, Oban, UK

<sup>2</sup>The Department of Geosciences, University of Edinburgh, Grant Institute, Edinburgh, UK

<sup>3</sup>Department of Earth and Planetary Sciences, The Johns Hopkins University, Olin Hall, 34th and North Charles Streets, Baltimore, MD 21218, USA

<sup>4</sup>Istituto di Scienze Marine, S.S. di Lerici, Consiglio Nazionale delle Ricerche, Forte Santa Teresa, Pozzuolo di Lerici, (SP), I-19032, Italy

## Key Points:

- Kangerdlugssuaq Glacier terminus regularly exposed to oceanic heating rate of 0.5 TW during winter.
- Wind forcing frequency is a crucial parameter in determining magnitude of heat exchange.
- Vertical mixing enhances buoyancy-driven overturning circulation.

## Abstract

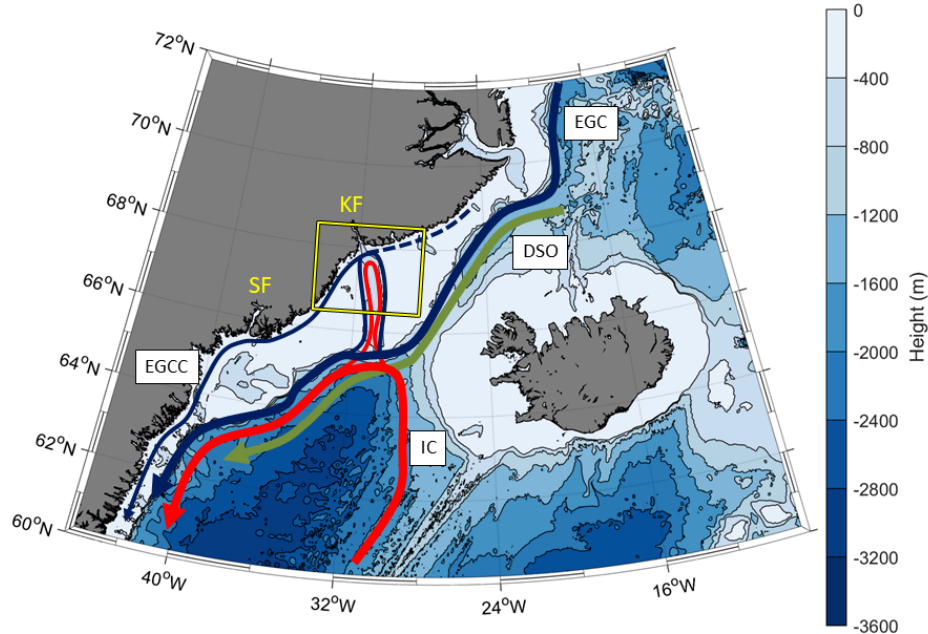
A realistic numerical model was constructed to simulate the oceanic conditions and circulation in a large southeast Greenland fjord (Kangerdlugssuaq) and the adjacent shelf sea region during winter 2007-2008. The major outlet glaciers in this region recently destabilised, contributing to sea level rise and ocean freshening, with increased oceanic heating a probable trigger. It is not apparent a priori whether the fjord dynamics will be influenced by rotational effects, as the fjord width is comparable to the internal Rossby radius. The modelled currents, however, describe a highly three-dimensional system, where rotational effects are of order-one importance. Along-shelf wind events drive a rapid baroclinic exchange, mediated by coastally trapped waves (CTWs) which propagate from the shelf to the glacier terminus along the right-hand boundary of the fjord. The terminus was regularly exposed to around 0.5 TW of heating over the winter season. Wave energy dissipation provoked vertical mixing, generating a buoyancy flux which strengthened overturning. The CTWs also acted to strengthen the cyclonic mean flow via Stokes' drift. Although the outgoing wave was less energetic and located at the opposite sidewall, the fjord did exhibit a resonant response, suggesting that fjords of this scale can also exhibit two-dimensional dynamics. Long periods of moderate wind stress greatly enhanced the cross-shelf delivery of heat towards the fjord, in comparison to stronger events over short intervals. This suggests that the timescale over which the shelf wind field varies is a key parameter in dictating wintertime heat delivery from the ocean to the ice sheet.

## 1 Introduction

Recent reduction in the mass of the Greenland Ice Sheet (GrIS) has been most profound near its edge, indicative of ocean triggered melting [*Rignot and Kanagaratnam, 2006; Nick et al., 2009*]. Coastal water temperature has increased contemporaneously [*Straneo et al., 2013; Khan et al., 2014*], however direct contact between the ocean and the GrIS is limited to glacier termini which are typically located within Greenland's fjords. A thorough understanding of the exchange flows between these fjords and the continental shelf is therefore critical for quantifying the ocean's impact on the GrIS.

One of the most acutely affected glaciers in the previous two decades is Kangerdlugssuaq Glacier (KG), which terminates at Kangerdlugssuaq Fjord (KF), and is one of the major outlet glaciers of southeast Greenland. KG destabilised in 2004-05, when the rate of discharge suddenly doubled [*Bevan et al., 2012*], and again in 2016-2017 [*Suzanne Bevan 2018, personal communication, 20th April*], with re-advance and slowing generally exhibited in the interim period [*Khan et al., 2014*]. KF is of length  $L \sim 80$  km and width  $W \sim 6-8$  km with a maximum depth of around 900 m and a sill depth of around 500 m. At the mouth, where it widens to around 20 km, the fjord meets the north end of Kangerdlugssuaq Trough (KT), a 600 m deep cross shelf channel (Figure 1). KT is a known pathway for ocean waters from the Irminger Sea [*Gelderloos et al., 2017*], and intersects the shelf break at its southern end. Here, Atlantic Water (AW, Conservative Temperature ( $\Theta$ )  $\sim 4.5 - 6.5^\circ\text{C}$ , Absolute Salinity ( $S_A$ )  $\sim 34.9 - 35.2 \text{ g kg}^{-1}$ ) flows from east to west in a branch of the North Atlantic Current known as the Irminger Current (IC). A second, seasonal pathway for IC water towards KF is north through the Denmark Strait and across the shelf, leading to a warmer AW layer in winter than in summer [*Gelderloos et al., 2017*]. South of the Denmark Strait, the IC is joined by the East Greenland Current (EGC), which transports Polar Water (PW,  $\Theta < 0^\circ\text{C}$ ,  $\sigma_\theta < 27.70$ ) from the Arctic Ocean. Alongside the EGC, the East Greenland Coastal Current (EGCC) transports PW southwards close to the coast. Dense bottom water, termed Denmark Strait Overflow Water (DSOW,  $\Theta < 0^\circ\text{C}$ ,  $34.9 < S_A < 35.2 \text{ g kg}^{-1}$ ,  $\sigma_\theta \geq 27.8$ ), also enters the region here, released over the Denmark Strait sill in periodic boluses [*Koszalka et al., 2013*].

Due to seasonal sea ice cover, observations of KF hydrography and circulation are biased towards the summer months, when freshwater runoff is strongest, and there is hence



45 **Figure 1.** Bathymetry of southeast Greenland seas, with the locations of KF and SF indicated, along with  
 46 the pathways of the IC, EGC, EGCC and Denmark Strait Overflow (DSO) and the model domain shown in  
 47 yellow.

71 a relatively large literature on the buoyancy-driven circulation in Greenland fjords [*Sciascia et al.*, 2013; *Cowton et al.*, 2015; *Carroll et al.*, 2016]. A recent study by *Moon et al.*  
 72 [2017] highlighted the importance of subsurface iceberg melt as a freshwater source in  
 73 major SE Greenland fjords. This is also seen in *Inall et al.* [2014], where the large residual  
 74 heat loss from PW is associated with iceberg melting within KF. In winter, when  
 75 runoff is at a minimum, other factors likely play a primary role in driving circulation. Re-  
 76 sults from Sermilik Fjord (SF) [*Straneo et al.*, 2010; *Jackson et al.*, 2014; *Sutherland et al.*,  
 77 2014a; *Sciascia et al.*, 2014; *Jackson and Straneo*, 2016], a similarly sized neighbour to  
 78 KF, indicate that intermediary circulation, a rapid baroclinic exchange regime triggered  
 79 by along-shelf (with shore to the right) barrier winds, is a significant driver of fjord-shelf  
 80 exchange. Enhanced wind stress drives coastward flow in the Ekman layer resulting in  
 81 downwelling of the pycnocline, followed by upwelling once the wind relaxes. In an idealised  
 82 modelling study into barrier wind forcing of the KF/KT system under winter clima-  
 83 tological conditions, *Fraser and Inall* [2018] (hereafter FI18) see baroclinic exchange flows  
 84 generated as the displacement of the pycnocline propagates in-fjord as a subinertial in-  
 85 ternal wave. As barrier wind events occur predominantly in the winter months [*Harden*  
 86 *et al.*, 2011], the capacity for this mechanism to draw warm ocean waters into contact  
 87 with glacier termini remains uncertain. Modelling studies of KF [*Cowton et al.*, 2016]  
 88 and SF [*Sciascia et al.*, 2014] have found that, while intermediary circulation provokes a  
 89 rapid baroclinic exchange, heat delivery to the glacier is small in comparison with values  
 90 recorded during summer simulations [*Cowton et al.*, 2015; *Sciascia et al.*, 2014] and field  
 91 campaigns [*Inall et al.*, 2014; *Sutherland et al.*, 2014a]. *Spall et al.* [2017] showed that  
 92 along-fjord katabatic winds, known as piteraq, can also drive significant exchange.  
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94 Two-dimensional overturning regimes, driven by either runoff or shelf exchange,  
 95 have been the main focus in previous studies of circulation in KF and SF. However, re-  
 96 cent observational [*Inall et al.*, 2014; *Sutherland et al.*, 2014b] and modelling [FI18] stud-

ies have indicated these fjords have the capacity for significant lateral velocity variability and recirculation. *Carroll et al.* [2017] saw a highly three-dimensional flow field develop in idealised broad fjord simulations forced by tides and freshwater input. The modelling study by FI18 found that horizontally sheared, geostrophically balanced flows dominate the mean wintertime circulation in KF and facilitate exchange, with the inflowing (outflowing) currents residing against the right-hand (left-hand) boundary looking into the fjord. Furthermore, the subinertial internal waves which drive intermediary circulation were coastal trapped waves (CTWs), with maximum amplitude against the eastern sidewall while propagating up-fjord. Similar three-dimensional internal waves were the focus of a recent combined numerical and analytical study by *Jackson et al.* [2018], who made significant progress in characterising their behaviour and influence on exchange. Such cross-fjord variability is only prominent in fjords wider than the internal Rossby radius of deformation,  $L_R$ . KF is approximately 6 km across, a width comparable with the Rossby radius of deformation of 8 km estimated under summer conditions [*Inall et al.*, 2014; *Sutherland et al.*, 2014a] and which could be even smaller under winter conditions. The potential for a three-dimensional flow field inside KF introduces complexity to the current understanding, and the implications for fjord-shelf heat exchange are not fully understood.

As well as inducing a dynamical response, barrier winds have been found to make enduring changes to the water column structure in the fjord mouth with considerable implications for subsequent exchange. FI18 found that simulations forced with wind events exhibited greatly enhanced vertical mixing in the fjord mouth due to subinertial internal wave activity. Transport in KT was also enhanced by barrier wind forcing, and the extent to which cyclonic circulation in KT penetrated the fjord mouth was increased. Together these factors acted to weaken the stratification in the fjord mouth and introduce a more shelf-like water column structure there, an artifact which remained after the dynamical response to wind forcing (i.e. internal wave activity) had decayed. At a later time, dense bottom waters circulating in KT were able to breach the KF sill and cause a deep water renewal event in the fjord, reminiscent of observations of DSOW within KF [*Inall et al.*, 2014]. In model runs where prevailing winds were held constant (without barrier wind events), the mouth, like the KF interior, remained strongly stratified due to the freshening influence of the glacier front, and was resilient to deep-layer exchange with KT.

In this study, we use an adapted version of the model presented in FI18 to study the circulation and exchange in KF during December, January and February (DJF) of 2007-08. While FI18 focussed on isolating the effect of barrier wind events against a backdrop of winter climatological conditions through the use of a control run, here we look to place their influence in the context of a realistic reconstruction of a winter season. We focus primarily on shelf exchange processes, with the aim of definitively answering the question “Is there potential for significant wintertime heat exchange between shelf and fjord?”. The model is equipped with a parametrisation of the KG glacier front (a heat sink and freshwater source) which generates output variables for glacial melt rates [*Cowton et al.*, 2015]. We therefore look for links between glacial melt and various potential drivers of circulation, particularly wind forcing on the shelf.

## 2 Methods

The model used was the MIT general circulation model, which solves the Boussinesq equations of motion using the finite volume method (MITgcm, *Marshall et al.*, 1997). In this study we also employed the hydrostatic approximation. Integration was performed by the ARCHER UK National Supercomputing Service (<http://www.archer.ac.uk>). The model grid and bathymetry was constructed exactly as described in FI18, and so is only briefly outlined here.

The model domain covers 66.38 – 68.5°N, 34.59 – 28.05°W (Figure 2). It captured KF with a horizontal resolution of 360 m and a vertical resolution of 10 m. The



148 grid spacing increased towards the southern, eastern and western boundaries, so that the  
 149 resolution on the shelf was relatively coarse with a maximum value of 4 km in the south-  
 150 east and southwest corners. Bathymetry for the shelf region was extracted from the 30-  
 151 arcsecond International Bathymetric Chart of the Arctic Ocean (IBCAO). Bathymetry for  
 152 the fjord interior was collected using a swath on the cruise JR106b to KF [Dowdeswell,  
 153 2004]. An idealised vertical ice front was placed at the northern boundary of the do-  
 154 main, south of the true KG terminus location, as in FI18. Initial and boundary conditions  
 155 were generated exactly using output from the model presented in Gelderloos *et al.* [2017],  
 156 which was used to simulate the wider Irminger Sea region for one year beginning 1st June  
 157 2007. The availability of this high-resolution forcing data was our motivation for select-  
 158 ing that particular winter for hindcasting. At material boundaries, no-slip conditions were  
 159 applied at cell bottoms and free-slip conditions were applied at sidewalls.

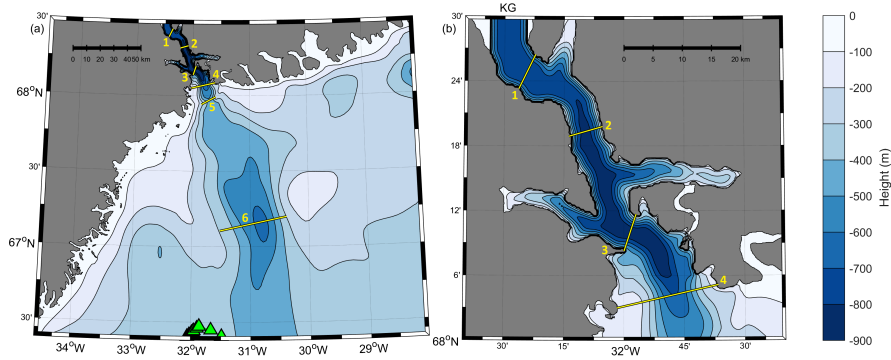
160 Wind and air-sea heat flux data were obtained from ERA-Interim 6-hourly and daily  
 161 reanalysis products [Dee *et al.*, 2011] respectively. Wind stress fields were calculated us-  
 162 ing the formula from Large and Pond [1981], which were then modified offline to reflect  
 163 local sea ice cover, as described in FI18, using temporally varying sea ice concentration  
 164 data obtained from the National Snow and Ice Data Centre (NSIDC). ERA-Interim wind  
 165 fields have been shown to resolve high-frequency katabatic winds in SE Greenland fjords  
 166 [Oltmanns *et al.*, 2014], giving confidence that this product is able to adequately capture  
 167 near-shore wind processes.

168 The MITgcm iceplume package [Cowton *et al.*, 2015] was employed to incorporate  
 169 the dynamical and thermodynamical effects of ice-sea interaction at the idealised KG ter-  
 170 minus. The package facilitates prescribed subglacial runoff, analytically solves the plume  
 171 equations from Jenkins [2011], and calculates local melting as a function of the tempera-  
 172 ture of the adjacent grid cells according to Holland and Jenkins [1999]. A minimum back-  
 173 ground velocity of  $0.02\text{m s}^{-1}$  was applied across the ice face [Cowton *et al.*, 2015]. Such a  
 174 parametrisation eliminates the necessity to run the model in non-hydrostatic mode by dis-  
 175 tributing resultant water masses at the level of neutral buoyancy. We took advantage of the  
 176 output variables for glacial melt rates provided by the iceplume package as an opportu-  
 177 nity to study correlations between glacial melt and fjord-shelf exchange forcings. However,  
 178 as we later discuss, the package was designed to describe the influence of the ice on the  
 179 water, not vice-versa, so we are cautious when interpreting variables related to glacier dy-  
 180 namics.

181 We employed the MITgcm implementation of the  $\kappa$ -Profile Parametrisation (KPP),  
 182 introduced by Large *et al.* [1994], which calculates the vertical mixing coefficient as a  
 183 function of the bulk Richardson number in the mixed layer and as a function of both the  
 184 local gradient Richardson number and parametrised double diffusion in the ocean interior,  
 185 where a constant is also added to represent internal wave breaking [Large *et al.*, 1994].  
 186 We used the Leith biharmonic scheme [Leith, 1996] to parametrise horizontal viscosity,  
 187 with nondimensional tuning coefficient  $\Lambda_4 = 1$  [Fox-Kemper and Menemenlis, 2008].

192 As the model by Gelderloos *et al.* [2017] was not of sufficient resolution to include  
 193 KF, the initial conditions within the fjord were horizontally extrapolated from the shelf.  
 194 A 100-day spin-up period was then carried out, with some runoff ( $100\text{m}^3\text{ s}^{-1}$ ) prescribed  
 195 evenly along the KG grounding line during the initial 60 days in order to allow an over-  
 196 turning circulation to develop within the fjord. This overturning then settled into a win-  
 197 tertime regime during the 40 days of spin up without runoff, sustained only by positive  
 198 meltwater feedbacks. Wind and boundary forcing were held constant at December 1st val-  
 199 ues during this period. The model was then integrated forwards using dynamic forcing  
 200 fields for 91 days, the duration of DJF 2007-08, with a timestep of 5 seconds.

201 *Harden et al.* [2011] define a barrier wind event as wind blowing from the north-  
 202 easterly quadrant, exceeding  $20\text{m s}^{-1}$ , and being distinct in time from other such events  
 203 by 24 h or more. According to this definition, nine barrier wind events occurred on the

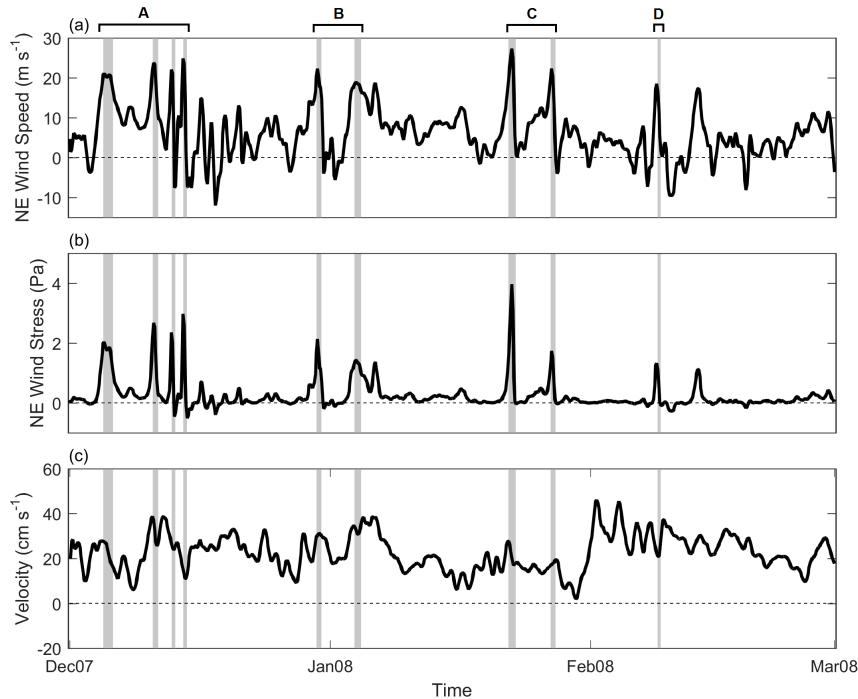


188 **Figure 2.** (a) Main model bathymetry, alongside (b) a zoom of the KF interior. Cross-fjord sections are  
 189 shown and numbered in yellow. Green triangles show the dive locations of an instrumented seal in January  
 190 2005, used here for model validation. The modelled location of KG is indicated outside the northern bound-  
 191 ary of the right-hand panel.

204 shelf outside KF in DJF 2007-08, and their occurrences are shown in Figure 3(a) along-  
 205 side northeasterly component of wind speed (note that this does not necessarily reflect the  
 206 *Harden et al.* [2011] definition threshold). The corresponding wind stress, which is usu-  
 207 ally quadratic in wind speed but becomes cubic when the wind exceeds  $11\text{ m s}^{-1}$  [*Large*  
 208 *and Pond*, 1981], is shown in Figure 3(b). Barrier wind events occurred less frequently dur-  
 209 ing DJF 2007-08 than is typical during DJF, with the number ranging from 7 to 20 dur-  
 210 ing 1989-2008 [*Harden et al.*, 2011]. Events were generally clustered in time, with four  
 211 events taking place in early December (hereafter Cluster A), two around the start of Janu-  
 212 ary (Cluster B), two towards the end of January (Cluster C), and one in mid-February  
 213 (Cluster D). Two of the wind events, the first in December and first in January, coincided  
 214 with prolonged periods of strong northeasterly wind stress, and were hence characteris-  
 215 tically different to the shorter peaks seen at other times. Both air and sub-surface water  
 216 temperatures were anomalously high in comparison with the 1981-2012 mean, though  
 217 consistent with other years since 2000 [*Khan et al.*, 2014]. Meridional velocity into KT  
 218 at the southern boundary is also an important external driver of dynamical variability, and  
 219 is shown in Figure 3(c). Barrier wind events regularly coincided with enhanced inflow  
 220 into the model domain, likely due to the intensification of barotropic currents on the shelf  
 221 by along-shore wind stress as described in *Nilsen et al.* [2016]. Notable exceptions arise  
 222 in late January and early February, however, when enhanced inflow did not coincide with  
 223 wind events, indicating that other factors also influence inflow variability.

### 229 3 Results and Analysis

230 We compared model diagnostics to various in situ measurements in order to gauge  
 231 model realism. With wintertime observations of the region scarce, no such data was avail-  
 232 able from within the model domain during the period of study. The vertical temperature  
 233 structure at 200-300 m depth (Figure 4, Sections 1, 2 and 3) agrees well with the moor-  
 234 ing record by *Jackson et al.* [2014] in 2009-10. We also utilised summertime observa-  
 235 tions from within KF, finding that the cross-sectional temperature structure in the model is  
 236 closely comparable to that observed in September 2010 by *Inall et al.* [2014] below around  
 237 250 m. Differences in stratification shallower than this depth are likely attributable to sea-  
 238 sonal variability in freshwater runoff. Some wintertime temperature and salinity data from  
 239 the shelf region of the model domain was obtained by an instrumented seal [*Treasure*  
 240 *et al.*, 2017] during the 4-5th January 2005. The seal performed 9 dives near the southern



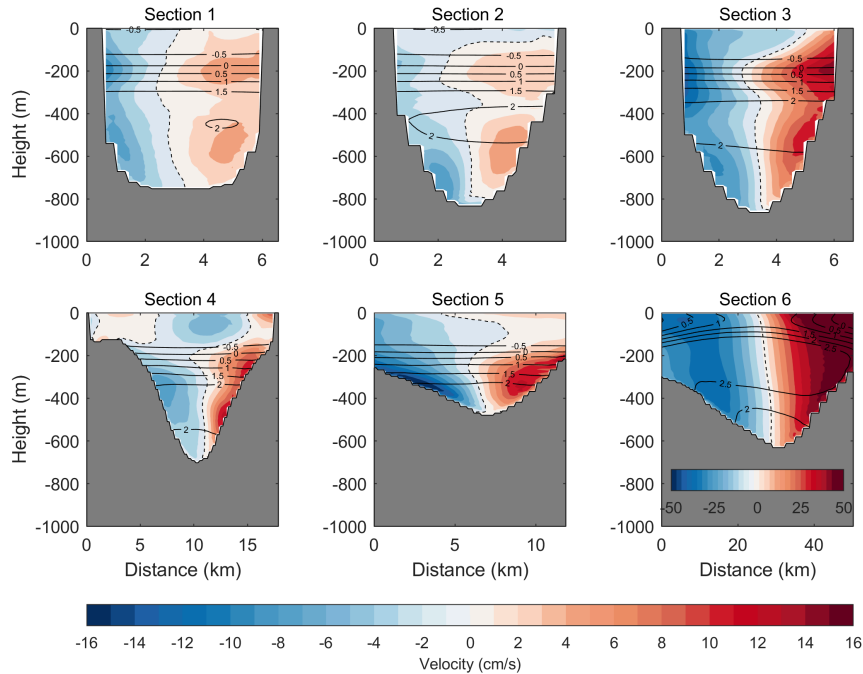
224 **Figure 3.** (a) Northeasterly component of wind speed (i.e. the component directed SW) over the deepest  
 225 point in KT (centre of Section 6). (b) Northeasterly component of wind stress over the deepest point in KT. (c)  
 226 Meridional velocity at the southern boundary taken from the core of the inflow into KT, defined as the region  
 227 where the mean flow exceeded  $20\text{ cm s}^{-1}$ . The greyed-out regions denote periods considered barrier wind  
 228 events by *Harden et al.* [2011], with wind event clusters labels at the top of the figure.

241 boundary (Figure 2), sometimes exceeding 300 m depth, giving temperature measurements  
 242 along its path. Figure S1 of the supplementary material shows the resulting temperature  
 243 field alongside the corresponding model temperature field for 4-5th January 2008, inter-  
 244 polated onto the seal's path. Overall, the model shows generally good agreement with the  
 245 observations in terms of stratification structure, thermocline height, and the temperature  
 246 in the upper and lower layers. The model does not reflect the sharp thermocline and sub-  
 247 surface temperature maximum seen at between 100 and 200 m depth in the observations,  
 248 while the surface waters (top 50 m) are also colder in the model. This may be due to in-  
 249 terannual variability as opposed to model inaccuracy. The close proximity to the model  
 250 boundary means that this agreement may be more a validation of the boundary conditions  
 251 than of the model itself.

252 The mean flow through six cross-sections of the combined KF/KT system is shown  
 253 in Figure 4, with mean isotherms overlaid. Section locations are shown in Figure 2. In  
 254 KT (Section 6) we see a strongly barotropic flow regime, with inflow (outflow) of around  
 255  $40\text{ cm s}^{-1}$  on the right (left) flank looking towards the fjord. In the fjord mouth (Sections  
 256 4 and 5) the mean flow is weaker and intensifies with depth, with current cores of around  
 257  $15\text{ cm s}^{-1}$  concentrated against sidewalls at around 400 m depth. Moving in-fjord the cur-  
 258 rents becomes weaker still, while retaining the pattern of inflow on the right and outflow  
 259 on the left. Isotherms reveal a strong thermocline (which coincides with the pycnocline,  
 260 not shown) within KF at a mean depth of around 200 m. Absolute geostrophic veloci-  
 261 ties (not shown), calculated using the sea surface height (SSH) and density fields at each

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section, are in close agreement with the modelled fields, indicating that the circulation is typically in geostrophic balance to a close approximation.

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**Figure 4.** Mean flow normal to standard cross sections shown in Figure 2. Black contours denote conservative temperature. Note the different velocity scale for Section 6.

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We computed the overturning streamfunction from the laterally-integrated along-fjord velocity field at each cross-section of the fjord interior (Figure 5), revealing any of the residual overturning circulation not obvious in the mean flow (Figure 4). At all sections, the time-mean streamfunction displays four local extrema, indicating a complex, multi-layered circulation scheme. The strength of overturning increases moving out of the fjord, most markedly between Section 2 and 3.

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Motivated by the barotropic nature of the flow in KT, we investigated the sea surface height (SSH) anomaly on Section 6 (relative to the spatio-temporal mean), looking specifically for correspondence between wind forcing and shoreward transport. Figure 6(a) shows the time evolution of SSH gradients alongside the depth-averaged current (DAC) normal to the section. The surface is generally depressed in the middle of the section and elevated at either side. Barrier winds regularly correspond to a deepening of the central depression, and appear to temporarily hinder the northward DAC on the eastern side while enhancing the the southward DACs in the western side. There is a marked discontinuity between the SSH structure in the first half of December and the rest of the simulation. We suspect this is due to either the influence of the erratic wind forcing during Cluster A (Figure 3) on the Ekman layer, an artefact of the southern boundary condition changing from static to dynamic at the beginning of the simulation, or both.

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Figure 6(b) shows the density anomaly at 300 m depth, which is approximately equivalent to the height of the pycnocline. Although temporal variability is greater than lateral variability, the  $1\sigma$  error bars indicate that density variability (and, hence, vertical motion of the pycnocline) is greatest towards the right-hand boundary of the fjord. The

289 right-hand side also corresponds to the greatest variability in along-fjord velocity in the  
290 lower layer.

297 From density profiles within the fjord, we obtained the horizontal velocity structure  
298 associated with normal baroclinic modes of oscillation [Emery and Thomson, 1997]. The  
299 linear, mode-one internal wave speed was  $c_1 = 1.1 \text{ m s}^{-1}$ , in agreement with Inall *et al.*  
300 [2014]. From this, we computed  $L_R = c_1/f = 8.1 \text{ km}$  and found the resonant seiche  
301 period to be  $T = 4L/c_1 \sim 3$  days.

302 We used empirical orthogonal function (EOF) analysis to isolate the statistically  
303 dominant modes of variability in the velocity field at each section of the KF interior (Sec-  
304 tions 1, 2 and 3) [Emery and Thomson, 1997]. Specifically, we note EOFs featuring a  
305 nodal contour corresponding to the zero-crossing in the first normal mode (around 200 m,  
306 approximately the mean pycnocline height). This pattern was seen in EOF 1 on Sections  
307 1 and 3, accounting for 31% and 49% of the variance at their respective locations (Figure  
308 7). On Section 2, this class of variability projected onto the second EOF which accounted  
309 for 30% of the total variance (the first EOF at Section 2, not shown, accounted for 37%  
310 of the variability and was similar in structure through more weakly sheared, with a nodal  
311 contour at around 350 m). In each of these fields, velocities above the pycnocline opposed  
312 those below, with strong vertical shear occurring at around 200 m depth. A similar verti-  
313 cal structure was found in the corresponding baroclinic normal modes of oscillation based  
314 on stratification (supplementary material, Figure S2), as in e.g. FI18; Sutherland and Stra-  
315 neo [2012]. This pattern of vertical variability is most intense adjacent to the eastern side-  
316 wall of the fjord and weakens toward the fjord interior. In Sections 2 and 3 this trend con-  
317 tinues to the western side of the fjord, while in Section 1 the pattern reverses west of the  
318 fjord centerline and intensifies again towards the western sidewall. The temporal variabil-  
319 ity of the EOF coefficient at each section was seen to increase with barrier wind forcing.  
320 As this was shown by FI18 in a very similar study, it is not shown again here.

323 Figure 8 shows a time series of horizontal velocity,  $(u, v)$  where  $u$  is the across-fjord  
324 component and  $v$  is the along-fjord component, averaged over the Section 2 lower-layer  
325 inflow region (defined as  $z < -200 \text{ m}$ ,  $\bar{v} > 3 \text{ cm s}^{-1}$ , Figure 4). Velocities are largely di-  
326 rected along-fjord, regularly alternating in sign. Cross-fjord velocities are maximal during  
327 these transitions, but are smaller by an order of magnitude. The largest along-fjord veloc-  
328 ities, along with the most frequent sign changes, generally occur in the days immediately  
329 following barrier wind event clusters on the shelf. During these times, the vectors describe  
330 a highly prolate ellipse.

334 Figure 9 shows a time series of the model-generated temperature profile 500m from  
335 the eastern boundary of Section 2. Quasi-periodic oscillations in the height of the ther-  
336 mocline persist throughout the simulation, although the shape, amplitude and frequency of  
337 the waveforms is highly variable. Furthermore, the thickness of the thermocline (defined  
338 as  $-0.5 < \Theta < 1.5^\circ\text{C}$ ) changes during the simulation, increasing from an initial value of  
339 around 50 m to reach almost 200 m, with a subsequent decrease coincident with increas-  
340 ing lower-layer temperature.

343 Wavelet analysis was used to decompose the velocity variability in frequency space.  
344 Similar to Fourier analysis, this method has the added advantage that the amplitude at  
345 each basis frequency may vary temporally, allowing a spectral perspective on the model's  
346 response to either stochastic or externally forced variability on the shelf. We performed  
347 the analysis on the along-fjord component of the Section 2 lower layer inflow (Figure 8),  
348 using a Morlet wavelet basis function (Figure 10; the different basis options are detailed  
349 in Torrence and Compo [1998] along with a comprehensive description of the procedure).  
350 The most significant harmonic variability occurs with period 2-4 days, consistent with the  
351 predicted resonant seiching period. There is a strong coincidence between barrier wind  
352 activity and excitation of this period band, with the frequency-averaged wavelet power  
353 exceeding the 95% confidence level on 4 occasions (Figure 10(c)), each corresponding

354 to a barrier wind event cluster. Harmonic variability also occurs with period  $\sim 25$  days,  
 355 which is broadly consistent with the interval between wind event clusters. However this  
 356 period lies largely within the cone of influence (Figure 10(a)), introducing the risk of spu-  
 357 rious signals due to edge effects, and does not exceed the 95% confidence interval (Figure  
 358 10(b)).

365 Defining exchange as

$$Q = \frac{1}{2} \iint |v(x, z)| dx dz \quad (1)$$

366 where  $x$  and  $y$  are the respective across- and along-fjord coordinates, we calculated  
 367 time series of the exchange through each cross-section (Figure S3, supplementary mate-  
 368 rial). In the fjord mouth (Sections 4 and 5) barrier wind events are commonly followed  
 369 by spikes in exchange, particularly following the first wind event of each cluster. The ex-  
 370 change through KT (Section 6) appears less sensitive to variability in wind patterns over  
 371 short timescales. The maximum correlation between the Section 5 and Section 1 time-  
 372 series occurred at a lag time of 14 hours, with a correlation coefficient of 0.94. The two  
 373 sections are approximately 55 km apart, indicating that information propagates up-fjord at  
 374 around  $1.1 \text{ m s}^{-1}$ , the predicted mode-one internal wave speed. This result holds for any  
 375 chosen pair of fjord cross-sections, though it is best seen when the sections are further  
 376 apart.

377 Defining advective heat flux as

$$Q_{\Theta} = C_p \rho_0 \iint v(x, z) \Theta(x, z) dx dz \quad (2)$$

378 where  $C_p$  is the specific heat capacity of seawater and  $\rho_0$  is reference density, we  
 379 calculated time series of the heat flux through each cross-section, shown in Figure 11.  
 380 The mean, standard deviation, and maximum heat flux values through each section are  
 381 shown in Table 1. Barrier wind activity generally results in an oscillating heat flux signal  
 382 at all locations, and hence the standard deviation is two orders of magnitude larger than  
 383 the mean at each section. The amplitude of the oscillation decreases by around a factor  
 384 of 10 between the fjord mouth and the fjord head. The response to each wind event is  
 385 inconsistent, differing in amplitude, frequency and number of cycles. For example, the re-  
 386 sponse to Cluster B is manifest as a relatively low-frequency oscillation, compared to the  
 387 responses to Clusters A, C and D. Furthermore, there is evidence of coherent signal prop-  
 388 agation which is not obviously caused by barrier wind forcing. Figure 12 shows the cumu-  
 389 lative time-integral of the heat flux plots shown in Figure 11. The maximum correlations,  
 390 with coefficient 0.27, between the heat flux timeseries at Section 5 and Section 1 suggest  
 391 a signal propagation speed of around  $1.5 \text{ m s}^{-1}$ , suggesting that the heat flux signal prop-  
 392 agates faster than the exchange signal. This may be a result of the heat flux signal being  
 393 driven by both intermediary circulation (propagating at  $1.1 \text{ m s}^{-1}$ ) and additional advection  
 394 by the cyclonic background flow (Figure 4).

401 We calculated the internal wave energy flux,  $\overline{v'P'}$ , through each cross-section, where  
 402  $v'$  and  $P'$  are the time-varying deviations from the mean along-fjord velocity and mean  
 403 pressure respectively [Nash *et al.*, 2005]. Figure 13 shows the time-mean energy flux through  
 404 each section. There is a net energy flux into the fjord through all sections, concentrated  
 405 on the right-hand side of the fjord at around 300 m depth. Incoming wave energy there-  
 406 fore corresponds to both up-fjord mean flow (Figure 4) and flow variability (Figure 7). It  
 407 is evident that the incoming wave is relatively nondispersive, with a maximum of around  
 408  $20 \text{ W m}^{-2}$  throughout the fjord (Sections 1-4). The significant down-fjord wave energy  
 409 flux on the left-hand side of Section 1 indicates that waves can propagate around the fjord  
 410 head efficiently. However, the outgoing wave energy flux decays quickly moving out fjord,



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**Table 1.** Mean, standard deviation, and maximum heat flux (TW) towards KG through each section.

Section no.	Mean	$\sigma$	Max.
1	0.003	0.185	0.540
2	0.012	1.022	2.275
3	0.014	1.608	3.894
4	0.019	2.254	7.294
5	0.171	2.567	8.580
6	0.572	15.61	36.00

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and by the fjord mouth (Section 4) is significantly smaller than the incoming flux. The time-mean energy flux through the fjord mouth (Section 4) was 2.7 MW (directed into the fjord).

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Subgrid-scale mixing parameters were calculated on the 300 m depth level, as this depth corresponds to a local maximum in both vertical and horizontal diffusivity which is not related to the surface or bottom boundary layers (Figure 14). The KPP-generated vertical diffusivity,  $\kappa_z$ , was greatest near the right-hand boundary near the fjord mouth and increased from a background value of around  $3 \times 10^{-4} \text{m}^2 \text{s}^{-1}$  in the fjord interior to around  $8 \times 10^{-4} \text{m}^2 \text{s}^{-1}$  following barrier wind events. Horizontal diffusivity,  $\kappa_h$ , which we recovered from the model-generated biharmonic viscosity according to *Fox-Kemper and Menemenlis* [2008], Equation 33, was more uniformly distributed in both space and time, although values were again higher near fjord sidewalls where the mean values were around  $2 \text{m}^2 \text{s}^{-1}$ .

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We investigated the role of shear dispersion a process whereby an effective horizontal diffusivity,  $\kappa_{sd}$ , is induced by vertical mixing in a vertically sheared flow. *Young et al.* [1982] estimate that in an oscillating flow,

$$\kappa_{sd} = \frac{1}{2} \left( \frac{\alpha}{\omega} \right)^2 \kappa_z \quad (3)$$

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where  $\alpha$  is the maximal velocity shear and  $\omega$  is the angular frequency of oscillation. From this expression, we found that the mean horizontal diffusivity increased by  $0.6 \text{m}^2 \text{s}^{-1}$  due to shear dispersion at 300 m depth, effectively doubling the mean value. Spatial patterns in shear dispersion are inherited directly from those in  $\kappa_z$ , resulting in a much greater contribution towards horizontal diffusivity at the right-hand boundary where values reached  $100 \text{m}^2 \text{s}^{-1}$ .

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Figure 15(a) shows the time-mean melt pattern on the ice face at the northern boundary of KF. Melting is small in the upper layer and increases with depth, peaking at 350 m where the time-mean melt rate is  $0.21 \text{m d}^{-1}$ . Melting is also weaker at the lateral boundaries of the ice face so that strong melting is concentrated in the middle of the ice face, where the melt rate reaches a maximum of  $1.0 \text{m d}^{-1}$ . This is likely due to the dependence on flow speed in the adjacent cells [*Cowton et al.*, 2015]. We generated a time series of face-averaged melting over the course of the simulation (Figure 15(b)). Variability in melting occurs on timescales of 2-4 days, corresponding to the dominant period of the internal wave field. We find a correlation coefficient of  $r = 0.86$  between time series in face-averaged melt rate and adjacent flow speed, while  $r = 0.30$  between melt rate and adjacent temperature. Although parametrised melt rate is explicitly dependent on both the temperature and the velocity adjacent to the ice face [*Jenkins*, 2011], the range of temper-

451 atures in direct contact with the ice is relatively small. Instead, the large changes in flow  
 452 speed at the head of the fjord make this the dominant control over melting in the model.

453 The melt rates were spatially integrated to find the total volume melted per unit  
 454 time,  $dV/dt$ , which was then converted into an effective heat delivery from the ocean to  
 455 the ice sheet using

$$Q_i = \frac{dV}{dt} \rho_i (C_i \Delta\Theta + L_i) \quad (4)$$

456 where  $\rho_i = 930 \text{ kg m}^{-3}$  is the density of ice,  $C_i = 2100 \text{ J kg}^{-1} \text{ K}^{-1}$  is the specific  
 457 heat capacity of ice,  $\Delta\Theta = 10 \text{ K}$  is the temperature below freezing point of the glacier,  
 458 and  $L_i = 334,500 \text{ J kg}^{-1}$  is the latent heat of melting ice. We obtain  $\overline{Q_i} = 1.7 \text{ GW}$   
 459 and  $Q_i^{max} = 4.6 \text{ GW}$ , indicating that over half of the net northward heat supply through  
 460 Section 1 (Table 1) goes towards melting ice. That the maximum value is two orders of  
 461 magnitude smaller than the maximum advective heat flux through Section 1 highlights the  
 462 large temporal variability in  $Q_\Theta$ .

## 466 4 Discussion

### 467 4.1 Cross-shelf Transport

468 The SSH and velocity fields on Section 6 show the mean flow to be largely barotropic  
 469 due to the lack of apparent vertical velocity shear (Figure 4), with cyclonic circulation  
 470 ( $> 50 \text{ cm s}^{-1}$ ) supplying shelf waters to the fjord mouth (Video 1, supplementary mate-  
 471 rial). Although the variability in along-KT transport appears relatively unaffected by wind  
 472 activity, barrier wind events generally coincide with local maxima in exchange,  $Q$  (Fig-  
 473 ure S3, supplementary material, Section 6), and local minima in heat flux,  $Q_\Theta$  (Figure 11,  
 474 Section 6). We interpret this as a first-order response to the offshore barotropic pressure  
 475 gradient caused by shoreward Ekman transport. The resulting offshore current superposes  
 476 with the cyclonic pattern in KT, temporarily weakening the inflow on the eastern side of  
 477 KT while strengthening the outflow (Figure 6). This provokes a decrease in northward net  
 478 heat transport in KT (Figure 12, Section 6).

479 Following Cluster B, the shoreward heat flux through Section 6 remains positive  
 480 throughout the first half of January (Figure 11). This period also corresponds to a small  
 481 but sustained increase in cross-shelf exchange at Section 6 (Figure S3, supplementary  
 482 material). The two wind events in Cluster B are maxima of long periods of generally  
 483 increased wind speed, and are hence different in character to most other barrier wind  
 484 events during the simulation, which were typically stronger, shorter gusts with a lifespan  
 485 of around 2 days. For example, the second wind event in Cluster B occurred during the  
 486 longest uninterrupted spell of northeasterly wind speeds in excess of  $10 \text{ m s}^{-1}$  during the  
 487 record, which lasted 3.75 days. The wind events during Cluster B were also weaker than  
 488 many others during the simulation (Figure 3(a-b)), barely meeting the criteria of  $20 \text{ m s}^{-1}$   
 489 set by *Harden et al.* [2011]. We investigated this further by decomposing the variability  
 490 of the 10 m northeasterly wind component (Figure 3(a)) into frequency space, once again  
 491 using wavelet analysis, which confirmed that Cluster B coincided with the most signifi-  
 492 cant low-frequency variability during the record (late December/early January, Figure S4,  
 493 supplementary material).

494 *Nilsen et al.* [2016] describe a mechanism whereby along-shelf winds (with coast  
 495 to the right) strengthen the cyclonic circulation within cross-shelf troughs and force the  
 496 currents to follow shallower isobaths in order to conserve potential vorticity. This relies  
 497 upon quasi-geostrophic theory and hence holds when the wind forcing is steady, or varies  
 498 on subinertial timescales. Assuming that the KT system behaves similarly, such a mecha-  
 499 nism would explain the period of sustained positive heat flux through KT in the first half

of January, when along-shelf winds were sustained and exhibited low-frequency variability. With temperatures in northern KT and the fjord mouth region increased, subsequent fjord-shelf exchange would have led to warming of the KT interior, as seen throughout January in Figures 9 and 12.

We therefore assert that, based on the model presented here, the response of the shelf circulation to wind forcing may be partitioned into two contrasting regimes: short ( $\leq 1$  day), strong gusts of along-shore wind act to disrupt cross-shelf transport in KT by altering the barotropic pressure gradient on inertial or superinertial timescales while, conversely, lower-frequency (or sustained) wind forcing provides sufficient time for the cyclonic circulation to adjust to the increased barotropic pressure gradient. In the second case, the enhanced barotropic circulation in KT acts to increase cross-shelf delivery of AW. This dependence of the heat supply to the fjord mouth on the behaviour of the wind field is not captured in previous modelling studies of wind-driven fjord-shelf exchange [Sciascia *et al.*, 2014; Cowton *et al.*, 2016], highlighting the advantages of the combined fjord-shelf domain employed here. Without this approach, the largest heat delivery events (following Cluster B, Figure 12) would not have been captured.

## 4.2 Circulation in the Fjord Interior

In accordance with intermediary circulation as outlined by Straneo *et al.* [2010] for SF, barrier winds initially produced a negative heat flux in the fjord interior due to upper-layer inflow, which model animations reveal to be a redirected branch of the EGCC (Video 2, supplementary material). This is followed by a positive contribution from lower-layer inflow (Video 2, Figure 11), and the expelled water in the upper layer rejoins the cold, coastal current.

The EOF patterns in Figure 7 are symptomatic of CTW activity, due to the intensification of flow variability towards the eastern side. We hence suggest that information about on-shelf wind variability propagates into the fjord interior in the internal wave field via subinertial CTWs. Video 1 (supplementary material) and Figure 16 give a qualitative description of the CTW structure, as vertical displacements in the  $S_A = 34 \text{ g kg}^{-1}$  isohaline surface (representative of the pycnocline) can be seen propagating from the shelf into the fjord along the right-hand boundary of the fjord mouth. Based on the model presented here, CTWs are the dominant mechanism for exchange in KF during the winter.

Inall *et al.* [2015] observed subinertial CTW behaviour in Kongsfjorden, a broad fjord in Svalbard, similarly forced by nonlocal wind activity. Carroll *et al.* [2017] see inertial Kelvin waves (i.e. CTWs at a vertical wall) arise via tide-sill interactions in idealised broad fjord models under summer conditions, without intermediary forcing. Similarly, Støylen and Weber [2010] see tidal generated CTWs emerge in a simulation of Van Mijenfjorden, Svalbard. This activity is hence not exclusive to SE Greenland and is seemingly the natural response, in broad fjords, to a variety of stimuli. CTWs are not captured in two-dimensional simulations of fjord-shelf exchange [Sciascia *et al.*, 2014] or using horizontally uniform boundary forcing at the fjord mouth [Cowton *et al.*, 2016], again illustrating that exchange between fjord and shelf is best understood when the two regions are considered in a single framework (as is also done in FI18 and Jackson *et al.* [2018]).

The model-generated mean advective heat flux values (Table 1) were generally consistent with FI18, further constraining estimates of the oceanic contribution to melting at KG during the winter months. While these values appear small in comparison to those of Cowton *et al.* [2016], who saw summer monthly mean values exceed 1 TW in KF, this is not a true comparison as Cowton *et al.* [2016] considered only the up-fjord heat flux as opposed to the net. The maximal values of 2.2 TW in the mid-fjord (Section 2) and 0.5 TW at the fjord head (Section 1) are in excess of observed values, which were taken in summer. Inall *et al.* [2014] reports 0.26 TW through an equivalent Section 2, while Sutherland *et al.* [2014a] report 0.003 and 0.19 TW through equivalent Sections 1 and 2

551 respectively. The high temporal variability, associated with CTW activity, highlights the  
 552 danger in taking synoptic sections of broad fjords as representative of the mean flow. The  
 553 strong resemblance between Figure 6 of *Inall et al.* [2014] and the EOFs shown in Figure  
 554 7 leads author MEI to re-emphasise that although in geostrophic balance, the reported heat  
 555 transport value of 0.26 TW from *Inall et al.* [2014] should be interpreted as a synoptic  
 556 value, that may alias some subinertial variability around an unknown mean. This consis-  
 557 tency between modelling and observational results further validates the model, and also  
 558 indicates that CTWs influence the KF circulation in summer. It is not clear how sensitive  
 559 these heat flux values are to the choice sub-grid scale mixing regime, which influences  
 560 nature of the flow field.

561 The broadly similar temporal patterns in the heat flux time series at each section  
 562 (Figure 11) indicate coherent communication between fjord and shelf. Although changes  
 563 in shelf temperature are quickly manifest in the fjord mouth and interior, the lag times be-  
 564 tween sections suggest that information of lower layer inflow/outflow propagates up-fjord  
 565 in the internal wave field as opposed to anomalous warm or cold patches advecting from  
 566 KT to the head of KF. The (time-mean) temperature field shows an along-fjord temper-  
 567 ature gradient in the lower layer (Figure 4), resulting in a reduced vertical temperature  
 568 gradient towards the fjord head. This is consistent with the order-of-magnitude decrease in  
 569 the scale of heat flux variability between the fjord mouth (Sections 4 and 5) and the head  
 570 of the fjord (Section 1). The decay in the heat-flux signal is hence greater than the decay  
 571 in wave-energy moving up-fjord (Figure 13). In the mid-fjord, along-fjord advection me-  
 572 diated by the internal wave field is associated with high-frequency variability in the heat  
 573 content of the water column throughout the simulation (Figure 9). However, it is follow-  
 574 ing the low-frequency Cluster B wind events, when an abundance of AW was present in  
 575 northern KT, that lower-layer temperatures are seen to increase most significantly and en-  
 576 duringly (Figure 9).

577 The Burger Number,  $Bu$ , captures the relative importance of stratification to poten-  
 578 tial vorticity over sloping topography:

$$Bu = \left( \frac{NH}{fL} \right)^2, \quad (5)$$

579 where  $N$  is the buoyancy frequency,  $f$  is the Coriolis parameter and  $H/L$  is the to-  
 580 pographic slope. The very high time-mean values of  $Bu \sim 400$  in the mid-fjord indi-  
 581 cate that the steep topography and strong stratification dominate over rotational effects. By  
 582 comparison, we obtained  $Bu \sim 0.8$  in KT, indicating that the weaker stratification and  
 583 shallower slope may introduce greater nonlinearity permitting rapid dispersion. Hence, we  
 584 observe a less distinct wave-like response in Section 6 of Figure 11.

585 It is illuminating to approximate these CTWs as Kelvin waves in a two-layer sys-  
 586 tem [FI18, *Jackson et al.* [2018]; *Støylen and Weber* [2010]; *Inall et al.* [2015]]. The ver-  
 587 tical pycnocline displacement,  $\xi$ , and the depth-integrated upper- and lower-layer veloci-  
 588 ties,  $(U_1, V_1)$  and  $(U_2, V_2)$ , of such a wave can be modelled analytically [*Støylen and Weber*,  
 589 2010; *Jackson et al.*, 2018] as

$$\xi(x, y, t) = Ae^{x/L_R - \beta y} e^{i(ky - \omega t)} \quad (6)$$

$$U_1(x, y, t) = -U_2(x, y, t) = 0 \quad (7)$$

$$V_1(x, y, t) = -V_2(x, y, t) = AC_1 e^{x/L_R - \beta y} e^{i(ky - \omega t)} \quad (8)$$

590 where the Cartesian basis orientation is as depicted in Figure 16 and  $x = 0$  is the  
 591 right-hand boundary. Here  $A$  is the wave amplitude,  $k$  is the wavenumber,  $\omega$  is the angu-  
 592 lar frequency and  $\beta$  is a longitudinal damping coefficient. Approximating  $U_1 = U_2 = 0$

593 appears justified, to first order, based on the small cross-fjord velocities in Figure 8. In  
 594 this simple, linear model, CTWs are nondispersive and hence propagate at the speed of  
 595 a mode-1 internal wave, consistent with the good agreement between the theoretical and  
 596 observed wave speed of  $c_1 = \omega/k = 1.1 \text{ cm s}^{-1}$ . Based on the significant response of the  
 597  $\omega \sim 3 \text{ rad d}^{-1}$  (Figure 10), we estimate  $k \sim 0.02 \text{ rad km}^{-1}$ . This corresponds to a wave-  
 598 length,  $\lambda = 4L \sim 240 \text{ km}$ , with  $L \sim 70 \text{ km}$  in our model. While this simple linear model  
 599 does not capture (nonlinear) amplitude dispersion, wave energy dissipation is described by  
 600 the parameter  $\beta$ . We observed wave amplitudes decay from  $A \sim 70 \text{ m}$  at the fjord entrance  
 601 (Section 4) to  $A \sim 50 \text{ m}$  at the fjord head (Section 1), two locations separated by a distance  
 602 of  $\Delta y \sim 55 \text{ km}$ , resulting in an estimate of  $\beta \sim 6 \times 10^{-6} \text{ m}^{-1}$ .

612 From Equations (6-8), CTW amplitude decays laterally on an  $e$ -folding length-scale  
 613 of  $L_R$ . In our case, with  $W/L_R \approx 1$ , amplitudes are hence significant at the opposing fjord  
 614 boundary, as is evidenced by Figure 6(b). We expect the incoming wave to have an ampli-  
 615 tude of  $A/e$  at the left hand boundary ( $\sim 25 \text{ m}$  at Section 3). Given a sufficiently strong  
 616 outgoing wave signal, the incoming and outgoing waves may therefore interact, resulting  
 617 in resonance (Figure 16). The opposing pattern found near the western bank of Section  
 618 1, EOF 1 (Figure 7) indicates that CTWs are either reflected or topographically steered  
 619 around the head of the fjord (in the  $\lambda \gg W$  regime we presume these two processes to  
 620 be roughly equivalent). However, the comparatively weak outgoing wave energy signal  
 621 in Sections (2-4) of Figure 13 indicated that the outgoing signal decays rapidly with in-  
 622 creasing distance from the glacier terminus. For a fjord cross section (arbitrarily taking  
 623 the section  $y = 0$ ) where the incoming and outgoing wave amplitudes are  $A$  and  $B$ , with  
 624  $A > B$ , the pycnocline displacement will be a superposition of the two signals:

$$\xi(x, t) = Ae^{x/L_R} e^{-i\omega t} + Be^{(W+x)/L_R} e^{-i\omega t} \quad (9)$$

625 We may have resonant motions if the condition  $Be \geq A$  is met in KF, or in general  
 626 if  $Be^{W/L_R} \geq A$ . This is demonstrated in Figure 16, where we expect a strong resonant in-  
 627 teraction in the interference zone (where the red and blue lines intersect). Consistent with  
 628 Equation 9, the shaded region in Figure 6(b) (representing the wave envelope at Section  
 629 2) is qualitatively comparable to the superposition of the incoming and outgoing wave en-  
 630 velopes. Velocity variability is dominated by the predicted resonant period band at Section  
 631 2 (Figure 10), reinforcing that this interaction plays a role in determining the timescales  
 632 for water mass exchange in KF. The importance of this interaction wanes moving out-  
 633 fjord, as  $A$  dominates over  $B$  due to wave energy dissipation.

634 Hence, while FI18 argued that KF was a broad fjord, evaluation of  $L_R$  here sug-  
 635 gests KF may be classified as an intermediate case between broad and narrow fjords, and  
 636 hence displays both broad- and narrow-fjord behaviour. The horizontally sheared mean  
 637 flow through all cross-fjord sections reaffirms the assertion, made by FI18, that rotational  
 638 effects are important, as expected in a broad fjord. Horizontal shear apparent in the snap-  
 639 shots of cross-sectional flow by [Cowton *et al.*, 2016] further indicate that the KF flow  
 640 field will tend towards three-dimensionality, even when conditions at the fjord mouth are  
 641 laterally uniform. At the same time, the strong response around the resonant frequency  
 642 would not be anticipated in the  $W/L_R \gg 1$  regime, where the incoming and outgoing  
 643 waves are spatially distinct and hence cannot interfere significantly. This result is con-  
 644 sistent with the theoretical predictions of [Jackson *et al.*, 2018], who find that rotational  
 645 effects are of order one importance when  $W/L_R > 0.5$

646 While Equations (6-8) appear to capture the wave mechanics to leading order, diver-  
 647 gences from this approximation are evident in our numerical model output due to nonlin-  
 648 ear effects and non-idealised stratification. While  $v$  dominates over  $u$  in Figure 8, the as-  
 649 sumption that  $u$  vanishes everywhere is clearly violated. The more sophisticated nonlinear  
 650 two-layer approach of Støylen and Weber [2010] is required to model these motions analyt-

651 ically, and although we do not follow this formulation here, we exploit some of the result-  
 652 ing outcomes. For example, the nonlinear approach of *Støylen and Weber* [2010] yields a  
 653 depth-averaged expression for Stokes' drift [*Stokes*, 1847],  $v_S$ , given by

$$v_S(x, y) = \frac{c_1 A^2}{2H_1^2} e^{2(x/L_R - \beta y)} \quad (10)$$

654 where  $H_1$  is the thickness of the upper layer. Evaluation of Equation 10 based on  
 655 the parameters in the model yields a Stokes' drift of  $v_S \sim 5 \text{ cm s}^{-1}$  at the fjord boundary,  
 656 decaying rapidly (with an  $e$ -folding length-scale of  $L_R/2$ ) moving toward the opposite  
 657 side. This is consistent with the horizontal structure seen in the model mean flow (Fig-  
 658 ure 4), while the vertical structure is consistent with the theoretical vertical structure for  
 659 Stokes' drift due to internal waves [*Wunsch*, 1973], with velocity maxima above and be-  
 660 low the wave energy maximum (Figure 13). Furthermore, the velocities are comparable  
 661 with the theoretical prediction of  $v_S \sim 5 \text{ cm s}^{-1}$  and, being quadratic in wave amplitude,  
 662 decrease moving in-fjord. This analysis reinforces the assertion made by FI18 that Stokes'  
 663 drift is a significant driver of the mean flow in KF and, by extension, other broad fjords  
 664 [*Støylen and Weber*, 2010; *Inall et al.*, 2015].

665 *Støylen and Weber* [2010] also show that boundary friction gives rise to significant  
 666 depth-averaged Eulerian drift,  $v_E$ , given by

$$v_E(x, y) = \sqrt{\frac{\beta}{C_D H_1}} e^{(x/L_R - \beta y)} \quad (11)$$

667 where  $C_D$  is the frictional drag coefficient. Based on a nominal value of  $C_D =$   
 668  $1 \times 10^{-3}$  [*Nost*, 1994; *Støylen and Weber*, 2010] we obtain an Eulerian drift of  $v_E \sim$   
 669  $0.5 \text{ cm s}^{-1}$ , an order of magnitude smaller than  $v_S$ . This contrasts the results of *Støylen*  
 670 *and Weber* [2010], who found  $v_E \sim 2v_S$ . This is likely due to the order-of-magnitude  
 671 difference in wave amplitude between this study and *Støylen and Weber* [2010], together  
 672 with quadratic amplitude dependence of  $v_S$ . The relatively high values of  $v_E$  reported  
 673 by *Støylen and Weber* [2010] are encountered under additional shear stress from fast ice  
 674 cover, which was not present in our model but is a known feature of KF during winter.  
 675 The effect may, therefore, be under-represented.

676 It is evident that two-layer approximations are not fully valid based on the stratifi-  
 677 cation in the model. For instance, in Section 2 of Figure 7 we see a three layer velocity  
 678 structure, which projects best onto the second normal mode (Figure S2). This is likely  
 679 due to the existence of a second, deeper thermocline due to isolated water below sill depth  
 680 (Figure 4). It is not clear, in this case, why Sections 1 and 3 exhibit a two-layer pattern.

### 681 4.3 Mixing in the Fjord Interior

682 The reversible nature of intermediary circulation (mediated here by CTWs) means  
 683 that for the process to generate non-zero time-integrated heat flux requires some mixing  
 684 in the fjord interior (excluding any heat lost to melting at the terminus). The temporal  
 685 divergences of the isotherms in Figure 9 imply that periods vertical mixing between the  
 686 PW and AW layers do occur, and are likely linked to stratified shear turbulence (Figure  
 687 14). CTWs hence drive both advection, which increases stratification, and mixing, which  
 688 decreases it. These two effects appear entangled such that it is hard to link the timing of  
 689 stratification changes in Figure 9 to wind forcing directly.

690 The cross-fjord structure of the wave energy flux (Figure 13) shows that the incom-  
 691 ing wave dominates over the outgoing wave, indicating that intermediary circulation driven



692 by CTWs is a non-adiabatic process where wave energy is lost to dissipation and mix-  
 693 ing. The net wave energy flux into the fjord implies that 2.7 MW is available for mixing  
 694 within the interior.

695 Shear dispersion was found to contribute significantly towards mixing in the model,  
 696 particularly concentrated against the right-hand boundary (Figure 14(b)). Since  $\kappa_{sd} \sim$   
 697  $1/\omega^2$ , we expect this mechanism to be highly effective in subinertial regimes such as  
 698 this. In contrast, much of the literature is concerned with near-inertial, tidal, or higher fre-  
 699 quency regimes [Støylen and Weber, 2010; Carroll et al., 2017] which will not have such a  
 700 prominent  $\kappa_{sd}$  component. Furthermore, the resonant value for  $\omega$  will be even smaller in  
 701 the reality, as KF is longer than represented in the model, indicating that shear dispersion  
 702 values may exceed the values in this study.

703 Integrating the buoyancy flux,  $\rho\kappa_z N^2$ , over the fjord interior, we obtained a time-  
 704 mean value of 1.25 MW. This represents the mean rate at which the potential energy of  
 705 the water column increased due to water mass transformation. Given the 2.7 MW of net  
 706 wave energy into the fjord, this implies a mixing efficiency of 0.46. This exceeds the typ-  
 707 ical literature value of 0.2 [Gargett, 1984], and is significantly higher than the value of  
 708 0.06 proposed for fjords by Stigebrandt [2012]. This high value is a result of the KPP  
 709 mixing scheme, which has previously been found to be overly diffuse in shallow or coastal  
 710 regions [Durski, 2004]. Nonetheless, we expect that 0.46 gives a reasonable upper bound  
 711 on the efficiency of internal wave-driven water mass transformation within a SE Greenland  
 712 fjord.

713 Integrating the diffusive vertical heat flux,  $C_p \rho \kappa_z \partial\theta/\partial z$ , over the 300 m depth surface  
 714 (at which time-mean values were maximal) gave a value of 3.7 GW. Hence, according to  
 715 our model, the dissipative heat flux between the AW and PW layers is comparable to the  
 716 advective heat flux towards KG (Table 1, Section 1).

717 The increase in the strength of out-fjord transport, moving away from the glacier  
 718 front (Figure 5), implies that water mass transformation in the fjord interior is as signif-  
 719 icant as that driven by plume dynamics at the terminus. The wind-driven component of  
 720 overturning is assumed to be negligible due to fast ice cover in the fjord interior. The  
 721 marked increase in overturning strength between Sections 2 and 3 is therefore attributed  
 722 to significant vertical density flux via diapycnal mixing. The two side fjords in this region  
 723 provide additional topographic boundaries for CTWs to follow, increasing the area avail-  
 724 able for mixing at sidewalls (Figure 14), and the complex coastline drives mixing around  
 725 features such as headlands. As diapycnal mixing is fed by incoming internal wave energy,  
 726 this result indicates that CTWs act to increase the overturning circulation. This effect is  
 727 likely exaggerated by a factor of two or more as a result of the high mixing efficiency in  
 728 the model. Furthermore, an overly diffuse model would likely act to strengthen longitudi-  
 729 nal wave decay, and therefore anticipate that true value of  $\beta$  may be larger than that stated  
 730 in the previous section.

#### 731 4.4 Melting at the Glacier Terminus

732 Cluster B coincided with the highest melt rates in the simulation (Figure 15). The  
 733 high melt rates preceded the large increase in heat content within KF (Figure 12), indicat-  
 734 ing that they are triggered by increased flow speed due to CTW propagation as opposed  
 735 to increased temperature. Given the close correlation between melt rate and adjacent flow  
 736 speed in the model, another potentially important factor is the capacity for CTWs to in-  
 737 duce energetic flow in the upper reaches of the fjord. The exchange flows triggered by  
 738 barrier wind forcing were in general found to decay considerably between the mid-fjord  
 739 and the fjord head, while the exchange flows triggered by Cluster B remained highly sig-  
 740 nificant at Section 1 (Figure S3, supplementary material). This effect may be greater in  
 741 the real KF, which is longer than the KF represented in the model. Theory shows maxi-  
 742 mum particle speed to be linear in amplitude for long waves [Cushman-Roisin and Beck-

ers, 2011], and we therefore attribute the strong melting to the large CTW amplitudes during Cluster B (Figure 9) as opposed to associated low-frequency  $Q_{\Theta}$  signal which continued throughout the first half of January.

The modelled melt rates of around of  $0.1 - 0.3 \text{ m d}^{-1}$  (Figure 15) are broadly consistent with *Cowton et al.* [2015] who, while introducing the iceplume package in an idealised fjord model, saw spatio-temporally averaged melt rates of  $0.18 \text{ m d}^{-1}$  in a model run without subglacial discharge. This value increased to  $0.22 \text{ m d}^{-1}$  when subglacial discharge was included, implying that the peaks in Figure 15(b) are comparable to summertime values. *Carroll et al.* [2016] found simulated summer melt rates (generated using the parametrisation by *Holland and Jenkins* [1999]) at KG to be an order of magnitude larger than the values reported here ( $\sim 4 \text{ m d}^{-1}$ ), although these values refer specifically to the locality of the subglacial plume rather than the spatial average over the ice front. Two-dimensional simulations of SF by *Sciascia et al.* [2014] saw melt rates (again from *Holland and Jenkins* [1999]) increase from  $\sim 0.2 \text{ m d}^{-1}$  in winter to  $\sim 2 \text{ m d}^{-1}$  with the addition of subglacial discharge, with the highest melt rates of all ( $2.2 \text{ m d}^{-1}$ ) recorded when subglacial discharge and intermediary circulation were simultaneously active. Due to the two-dimensional configuration, all melting was essentially restricted to the plume location in freshwater forced runs, which may explain the discrepancy with *Cowton et al.* [2015] and the (order-of-magnitude) agreement with *Carroll et al.* [2016]. The two-dimensional approach permits only vertical velocities next to the ice front, making buoyant subglacial plumes the primary agent for flow-dependant melting. While this is appropriate when  $W/L_R \ll 1$  [*Straneo et al.*, 2010; *Sciascia et al.*, 2013, 2014], the circulation described in this study suggests there is a mean (horizontal) flow across the front of the KG terminus and that, in broader fjords, large flow speeds can occur next to the ice face in the absence of freshwater forcing. Systems in this category therefore require a three-dimensional description in order to fully characterise and compare summertime and wintertime melting.

While the heat delivery to the ice sheet,  $Q_i$ , was consistent with the mean advective heat flux towards the glacier,  $Q_{\Theta}$ , the modelled melt rates were two orders of magnitude smaller than the glacial flow speed at KG during 2007-08, which was around  $25 \text{ m d}^{-1}$  [*Bevan et al.*, 2012]. Our results therefore appear to suggest that ocean-driven melting during the winter was not capable of matching the rapid flow speeds observed during this period. We suspect, however, that our model under-represents the oceanic contribution to KG frontal ablation. This is primarily a study of shelf-driven exchange, and the model lacks the sophistication to produce realistic glacier diagnostics. The iceplume package was utilised to provide a heat sink at the head of the fjord and add a level of realism to hydrography in the far field. The package is highly sensitive to the prescribed background velocity when subglacial discharge is small or zero [*Cowton et al.*, 2015], as was the case here. Due to the static ice face geometry, the model cannot account for the triggering of calving events or instabilities in glacial flow due to ocean-driven melting at the terminus. The pattern of melting found on the ice face (Figure 15(a)) would in reality drive undercutting and hence encourage calving events. Furthermore, the flat ice face likely does not affect the adjacent flow realistically, as tidewater glacier termini are typically crevassed and uneven over small spatial scales. This may have caused the model to exaggerate the relative influence of adjacent flow speed over temperature.

## 5 Summary

A high-resolution numerical model of KF and the adjacent shelf region during winter 2007-08 shows coherent communication between fjord and shelf, with temperature changes on the shelf able to influence the fjord interior. AW is delivered from the shelf break towards the fjord by the geostrophically balanced cyclonic circulation in KT, which is driven by sea surface tilt. The mean circulation structure in KF is similar, though weaker and with a larger baroclinic contribution, and delivers heat to the glacier terminus due to mean cross-fjord temperature gradients. Water mass transformation due to melting at the

795 glacier front and mixing in the fjord interior adds a buoyancy-driven overturning compo-  
 796 nent to the circulation, although it is the horizontal shear which dominates the mean flow.  
 797 CTWs, which are instigated by barrier winds on the shelf, emerge as the dominant mode  
 798 of variability within the fjord and drive greatly enhanced along-fjord volume and heat  
 799 transport. CTWs also act to enhance both the buoyancy-driven overturning circulation, via  
 800 diapycnal mixing, and the cyclonic background flow, via Stokes' drift. The mechanism has  
 801 previously been observed in a broad, glaciated fjord in Svalbard [Inall *et al.*, 2015] and is  
 802 likely to play a significant role in broad fjords in general.

803 SE Greenland coastal waters have warmed in recent years, and we have demon-  
 804 strated here that barrier wind-driven CTWs have likely played a crucial role in commu-  
 805 nicating this ocean warming to the GrIS. The efficacy of CTWs in delivering heat towards  
 806 the KG terminus, in a time-mean sense, is highly dependent on the temporal variability  
 807 of barrier wind forcing. Typically barrier wind events are short and strong, ramping up  
 808 quickly and exceeding the  $20\text{m s}^{-1}$  threshold for only  $\sim 6$  h. However, this class of wind  
 809 forcing was not found to significantly increase fjord heat content. Rather, long-duration  
 810 northeasterly wind forcing was found to strengthen the barotropic circulation in KT, in-  
 811 creasing AW transport towards the fjord mouth, while provoking low-frequency CTWs  
 812 which are highly effective at drawing these waters up-fjord. This result points to barrier  
 813 wind duration, as opposed to strength, as the controlling parameter on the wintertime heat  
 814 delivery towards the GrIS.

815 The results indicate that significant oceanic heat ( $\sim 0.5$  TW) is regularly delivered  
 816 from the shelf to glacier terminus during winter. The CTW exchange process is driven  
 817 purely by shelf exchange and, although there may be some freshwater runoff in the winter  
 818 months, this is not a necessary condition for this magnitude of heat exchange. We have  
 819 encountered strong evidence that the processes occurs in the non-winter months, though it  
 820 is likely weaker and may be obscured or augmented by increased freshwater-driven over-  
 821 turning. Further research is required to fully understand the interaction between these two  
 822 circulation schemes.

823 While the model was able to provide diagnostics for melt rate at the KG terminus,  
 824 yielding a mean melt rate of  $0.21\text{m d}^{-1}$  at the centre of the ice face, the simplified param-  
 825 eterisation was unable to describe the glacial impacts of ice-ocean interaction in detail.  
 826 Coupled ice-ocean models, capturing glacier dynamics, calving, ice face texture and ma-  
 827 rine icebergs, are needed to significantly further our understanding of the rapid accelera-  
 828 tion and retreat of Greenland's tidewater glaciers.

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 834 may be obtained at <https://erddap.sams.ac.uk/erddap/files>.

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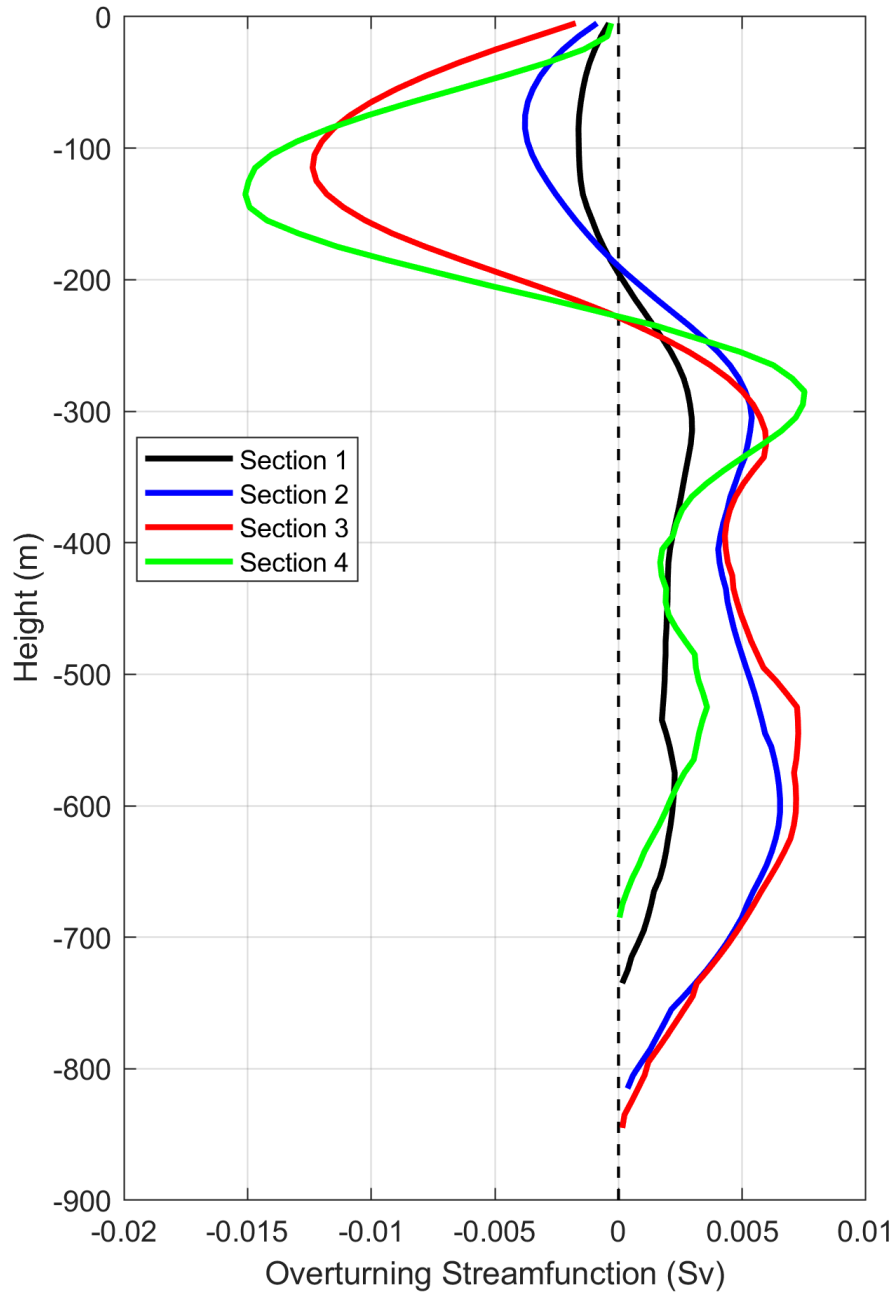
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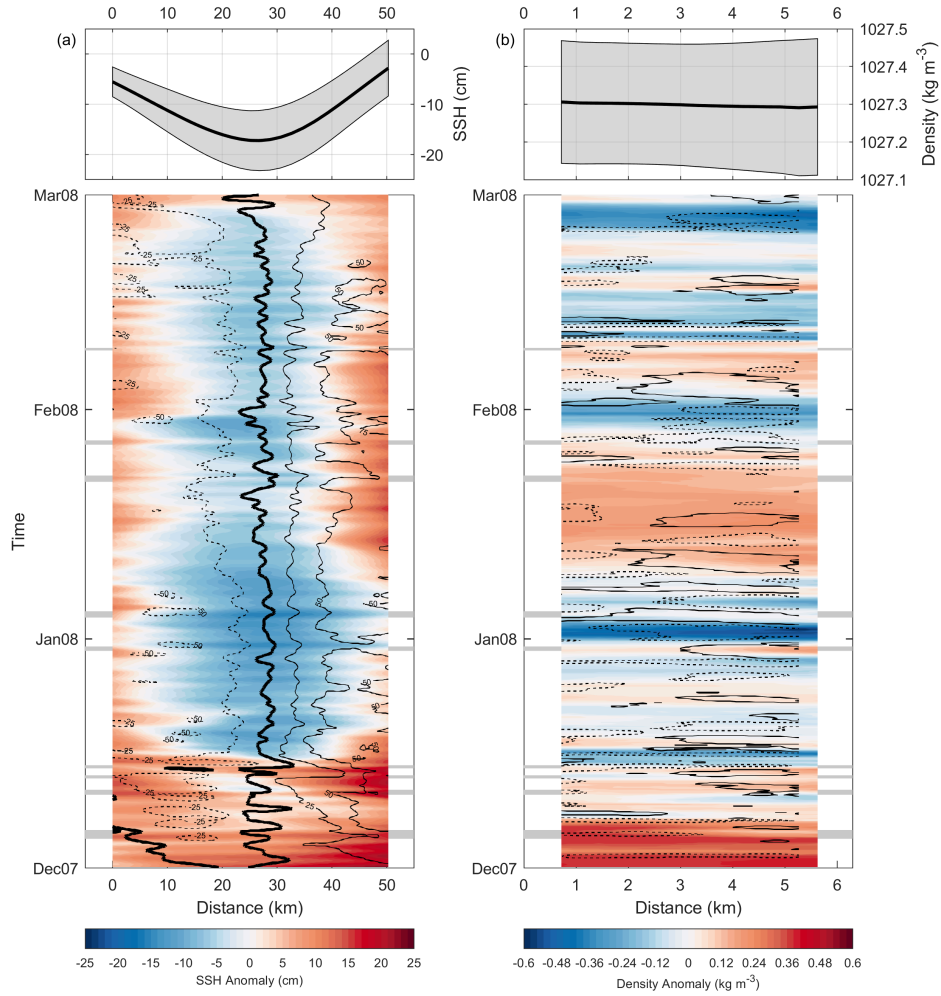
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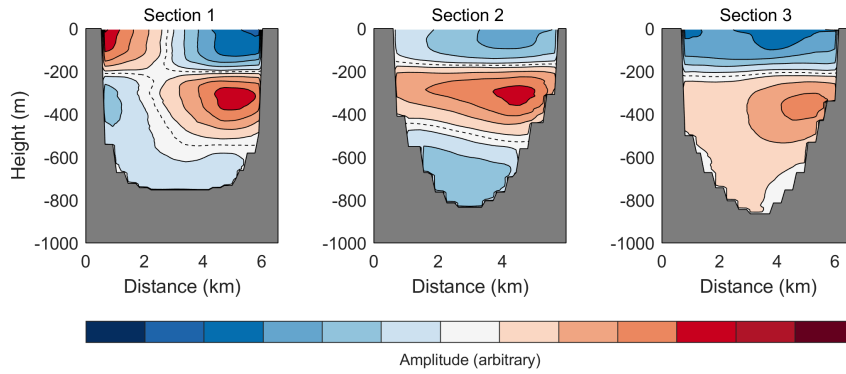


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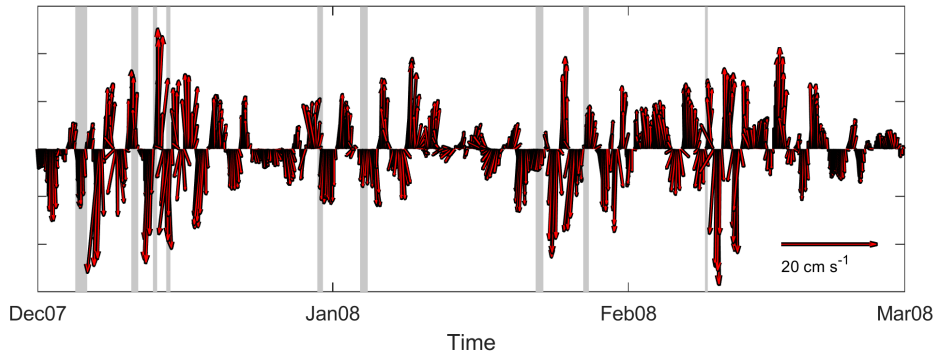
**Figure 5.** Mean overturning streamfunction at Sections 1-4. Positive here indicates up-fjord transport.



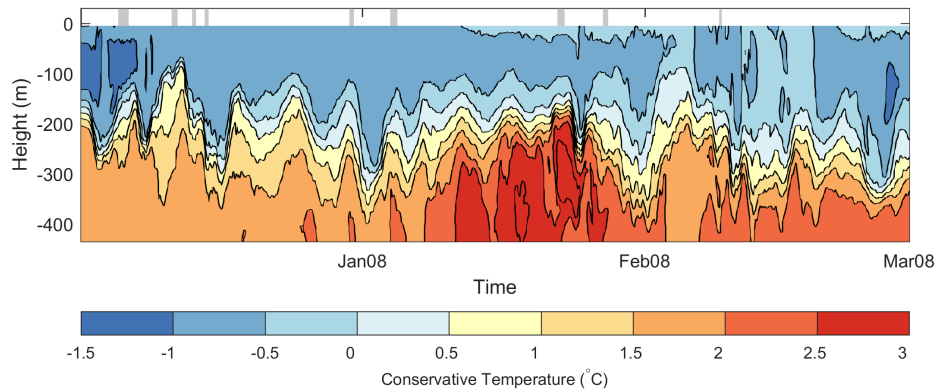
291 **Figure 6.** (a) Hovmöller diagram showing the SSH anomaly at Section 6 over the course of the simula-  
 292 tion. Solid (dashed) black lines denote northward (southward) DAC contours ( $\text{cm s}^{-1}$ ), while the bold black  
 293 line denotes zero DAC. The panel at the top shows mean SSH  $\pm 1\sigma$ . (b) Hovmöller diagram showing the  
 294 density anomaly at 300 m depth on Section 2 over the course of the simulation. Solid (dashed) black lines  
 295 denote northward (southward)  $10 \text{ cm s}^{-1}$  velocity contours at 400 m depth. The panel at the top shows the  
 296 corresponding mean density  $\pm 1\sigma$ . The bars down either side of each panel denote barrier wind activity.



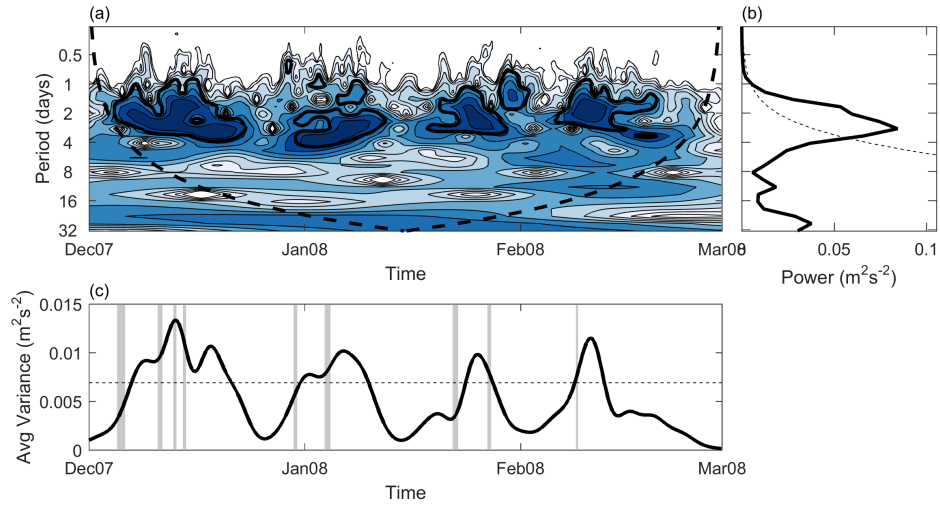
321 **Figure 7.** EOF 1 at Sections 1 and 3, and EOF 2 at Section 2, accounting for 31%, 49% and 30% of the  
 322 velocity variability at Sections 1-3 respectively. Here red opposes blue, while white represents no motion.



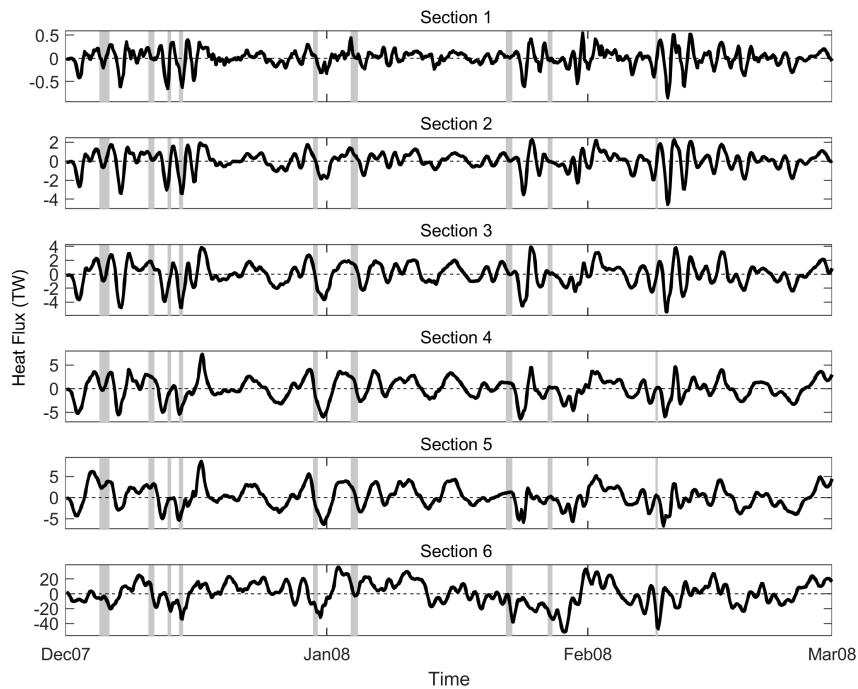
331 **Figure 8.** Horizontal velocity time series, averaged over the deep layer inflow region of Section 2. The  
 332 y-axis represents along-fjord velocity (normal to section) and the x-axis shows across-fjord velocity (parallel  
 333 to section). The greyed-out regions denote periods considered barrier wind events on the shelf



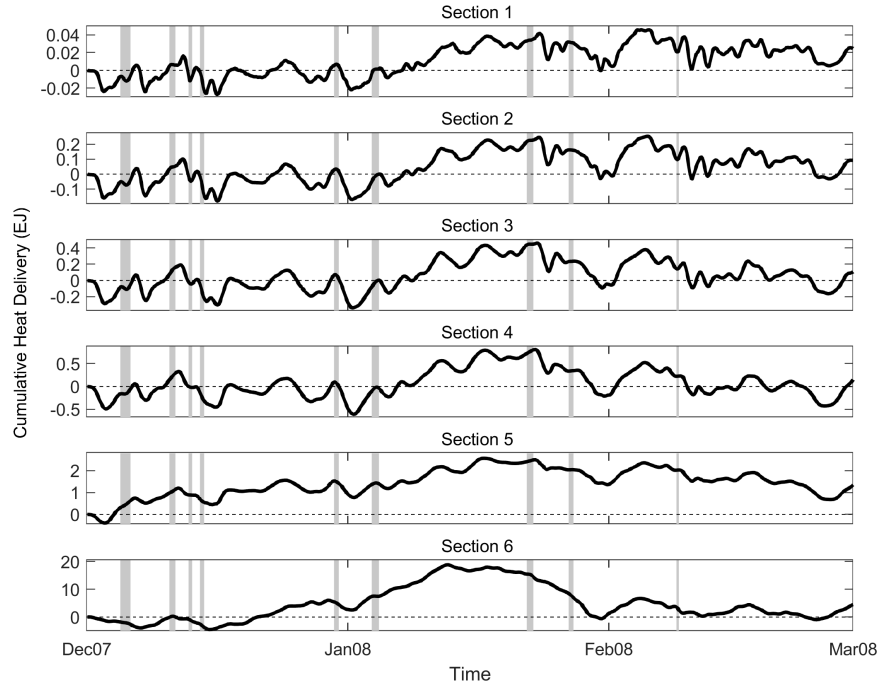
341 **Figure 9.** Temperature profile time series near the eastern end of Section 2. The grey bars at the surface  
 342 denote barrier wind events on the shelf.



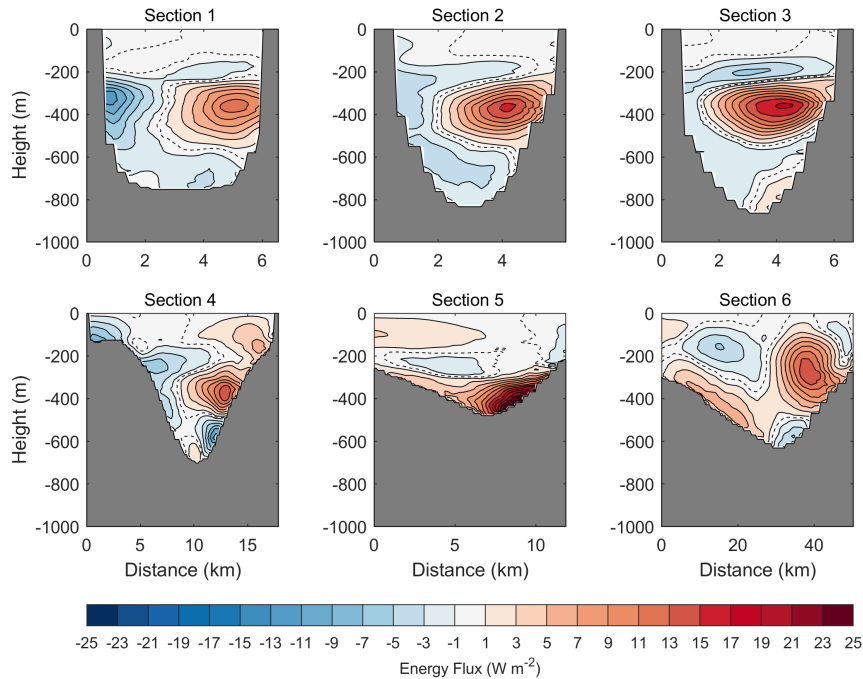
359 **Figure 10.** (a) The local wavelet power spectrum from velocity variability at the Section 2 lower layer in-  
 360 flow region, thick black contours enclose regions of 95% confidence or greater while the the region below the  
 361 dashed line is the cone of influence, where we expect edge effects to become important; (b) the Fourier power  
 362 spectrum, where the dashed line represents the 95% confidence level; (c) Frequency-averaged wavelet power,  
 363 with the dashed line representing the 95% confidence level. The greyed-out regions denote periods considered  
 364 barrier wind events on the shelf



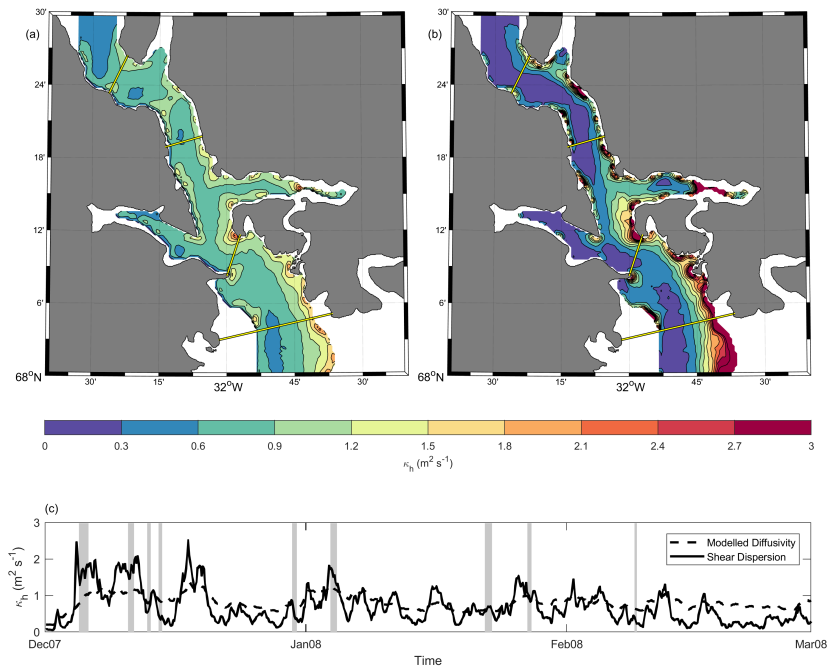
396 **Figure 11.** Heat flux through each of the standard cross sections of the KF/KT system. Note the different  
 397 ordinate scales. The greyed-out regions denote periods considered barrier wind events on the shelf.



398 **Figure 12.** Time-integral of the heat delivered through each of the standard cross sections of the KF/KT  
 399 system. Note the different ordinate scales. The greyed-out regions denote periods considered barrier wind  
 400 events on the shelf.

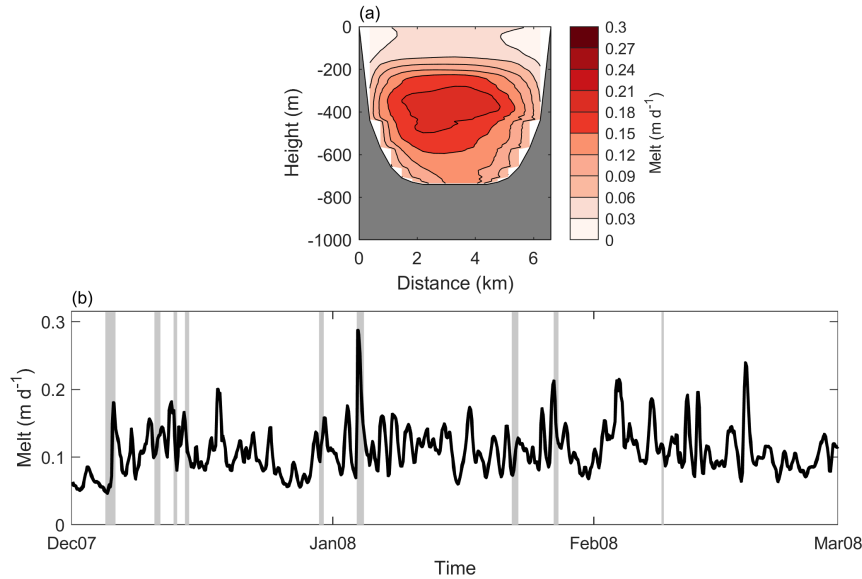


414 **Figure 13.** Time-averaged wave energy flux through each cross-section, with positive values indicating  
 415 energy flux into the fjord and a dashed line denoting the zero contour

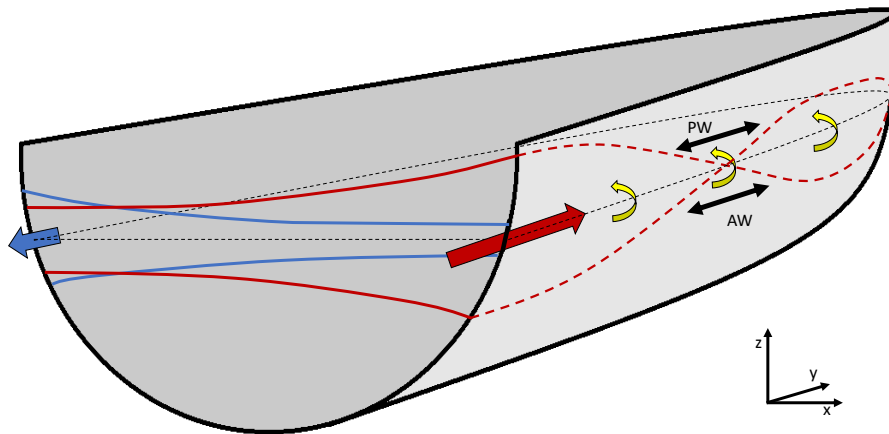


435 **Figure 14.** Mean subgrid-scale horizontal diffusivity at 300 m depth (a) from model generated fields and  
 436 (b) from shear dispersion (vertical diffusivity can be recovered approximately by dividing the shear dispersion  
 437 values by 2500). (c) Corresponding timeseries of the spatially averaged values. The greyed-out regions denote  
 438 periods considered barrier wind events on the shelf.





463 **Figure 15.** (a) Time-averaged melt rate simulated at the glacier terminus during DJF 2007-08. (b) Time-  
 464 series of spatially averaged melting. The greyed-out regions denote periods considered barrier wind events on  
 465 the shelf.



603 **Figure 16.** Schematic showing CTW activity in an idealised, Northern Hemisphere fjord where  $L_R/W \approx 1$ .  
 604 The neutral pycnocline height is indicated in dashed black. The red (blue) arrow indicates the propagation  
 605 of incoming (outgoing) wave energy, and is located at the wave amplitude maximum. Solid red (blue) lines  
 606 indicate the cross-sectional incoming (outgoing) wave envelope. Notice that wave energy decay effectively  
 607 moves the interference zone (where the red and blue lines intersect) to the left of the fjord centreline. The  
 608 dashed red lines show the longitudinal structure of the incoming wave at the right-hand boundary, with black  
 609 arrows denoting the associated velocities in the PW and AW layers. Note that these velocities oppose each  
 610 other and reverse over the course of a wave cycle. The yellow arrows represent shear-driven diapycnal mixing  
 611 and associated strengthening of the overturning circulation.

Figure 1.

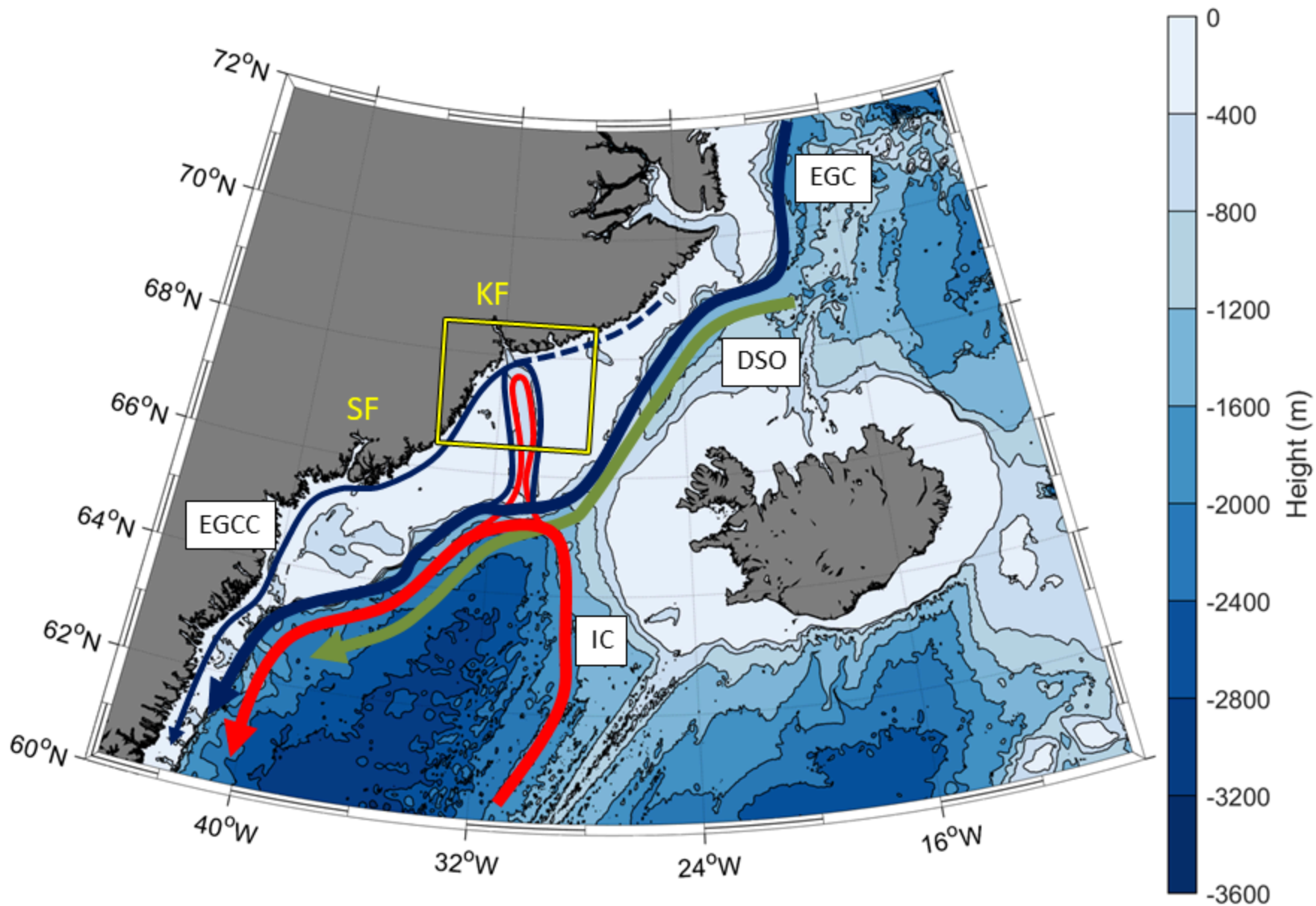


Figure 2.

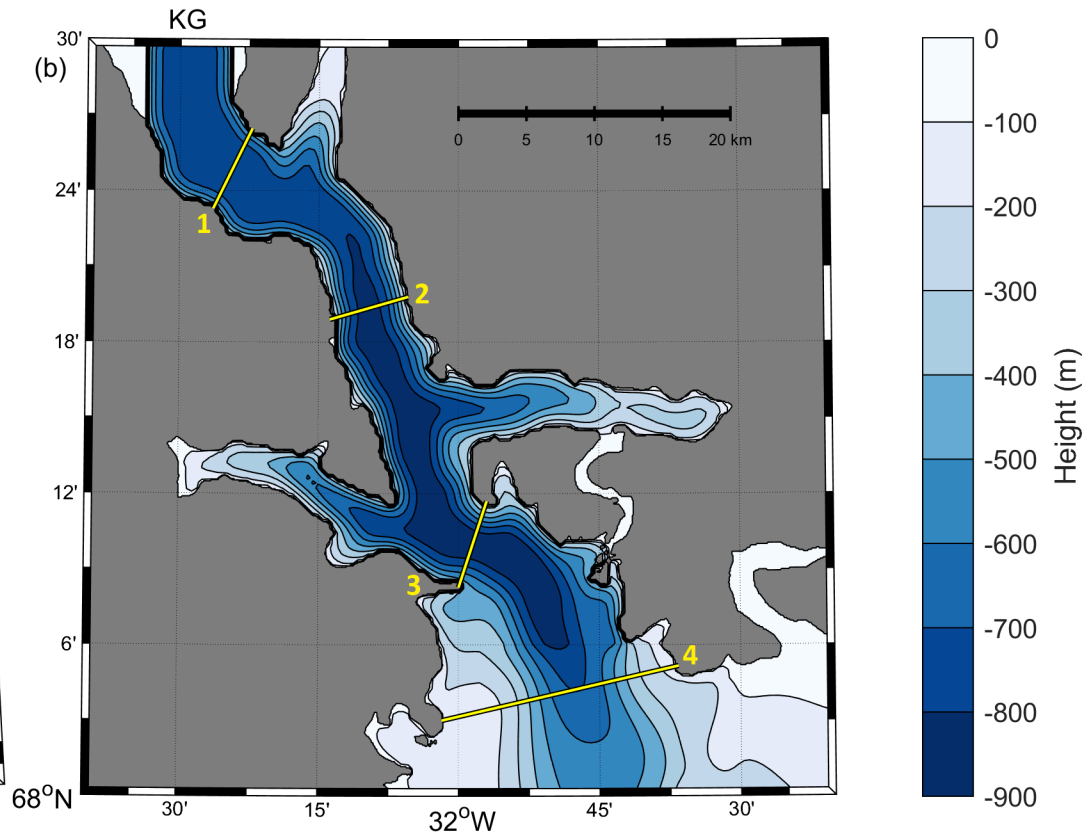
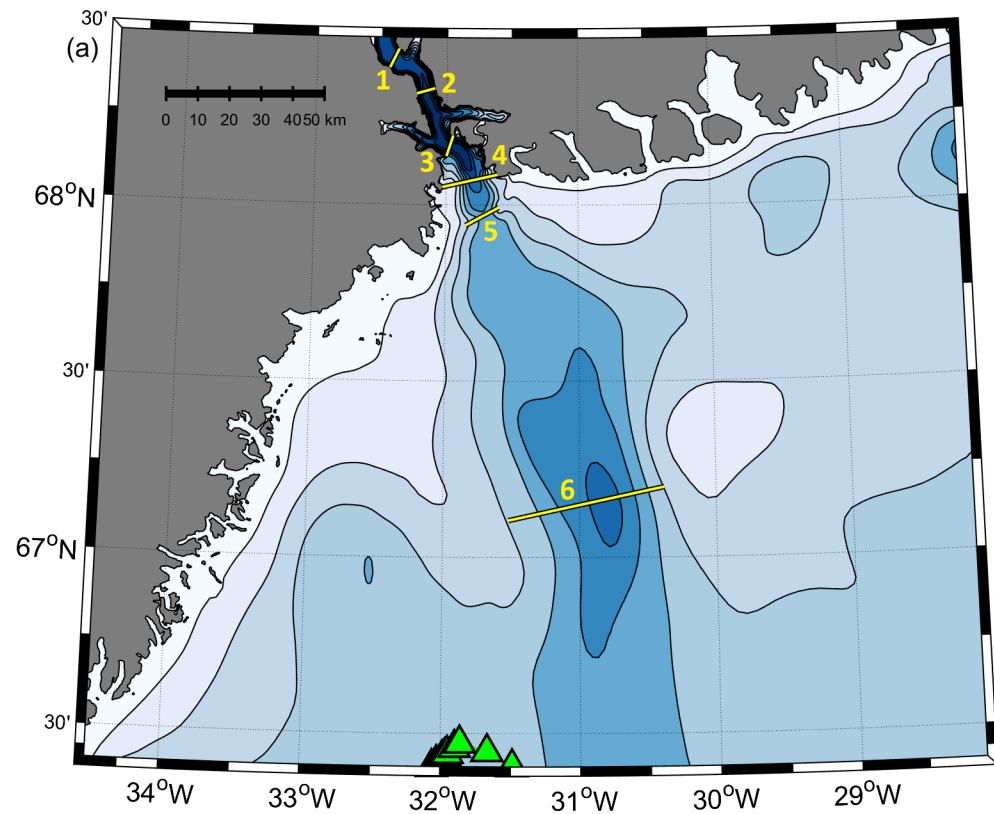
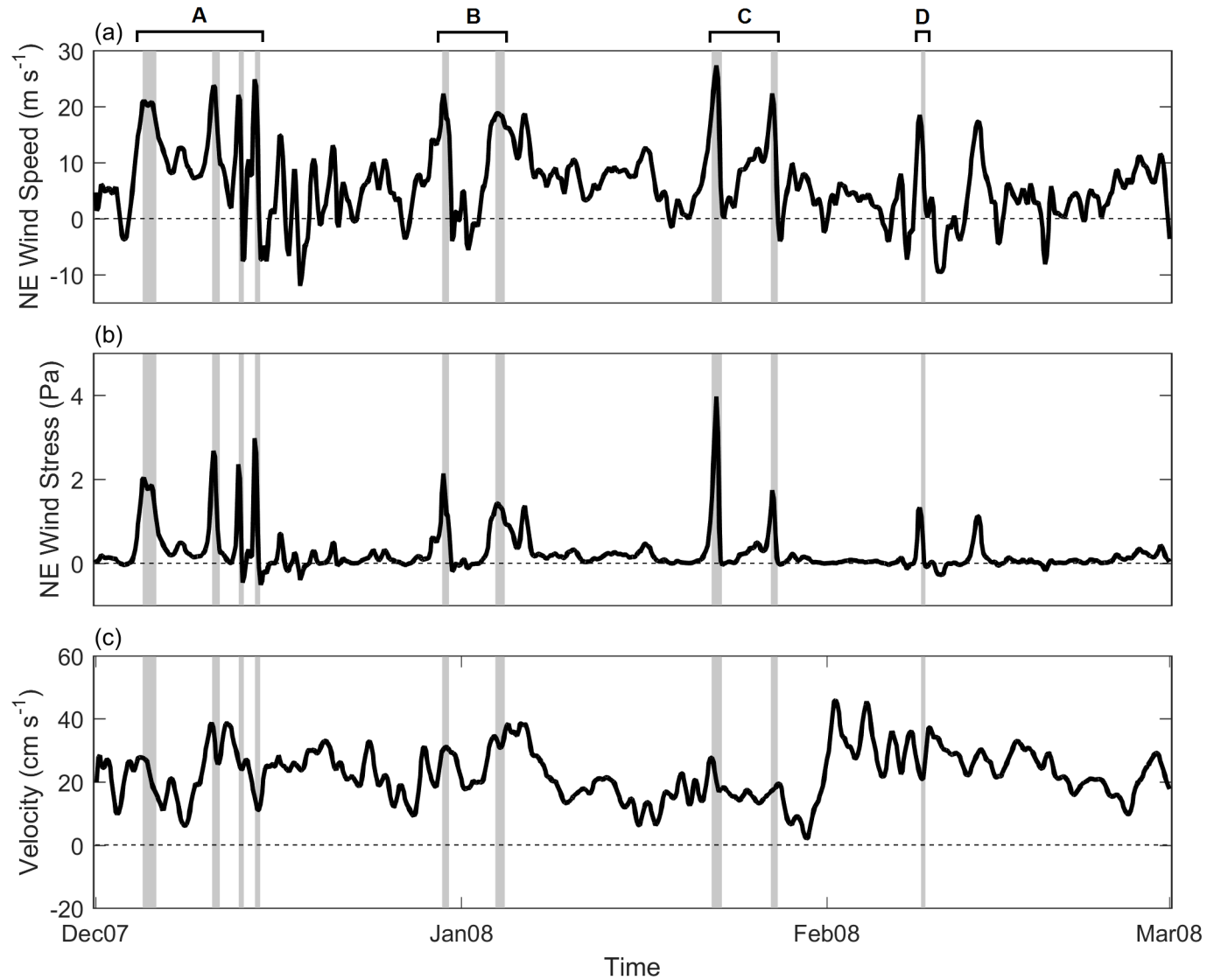


Figure 3.





**Figure 4.**

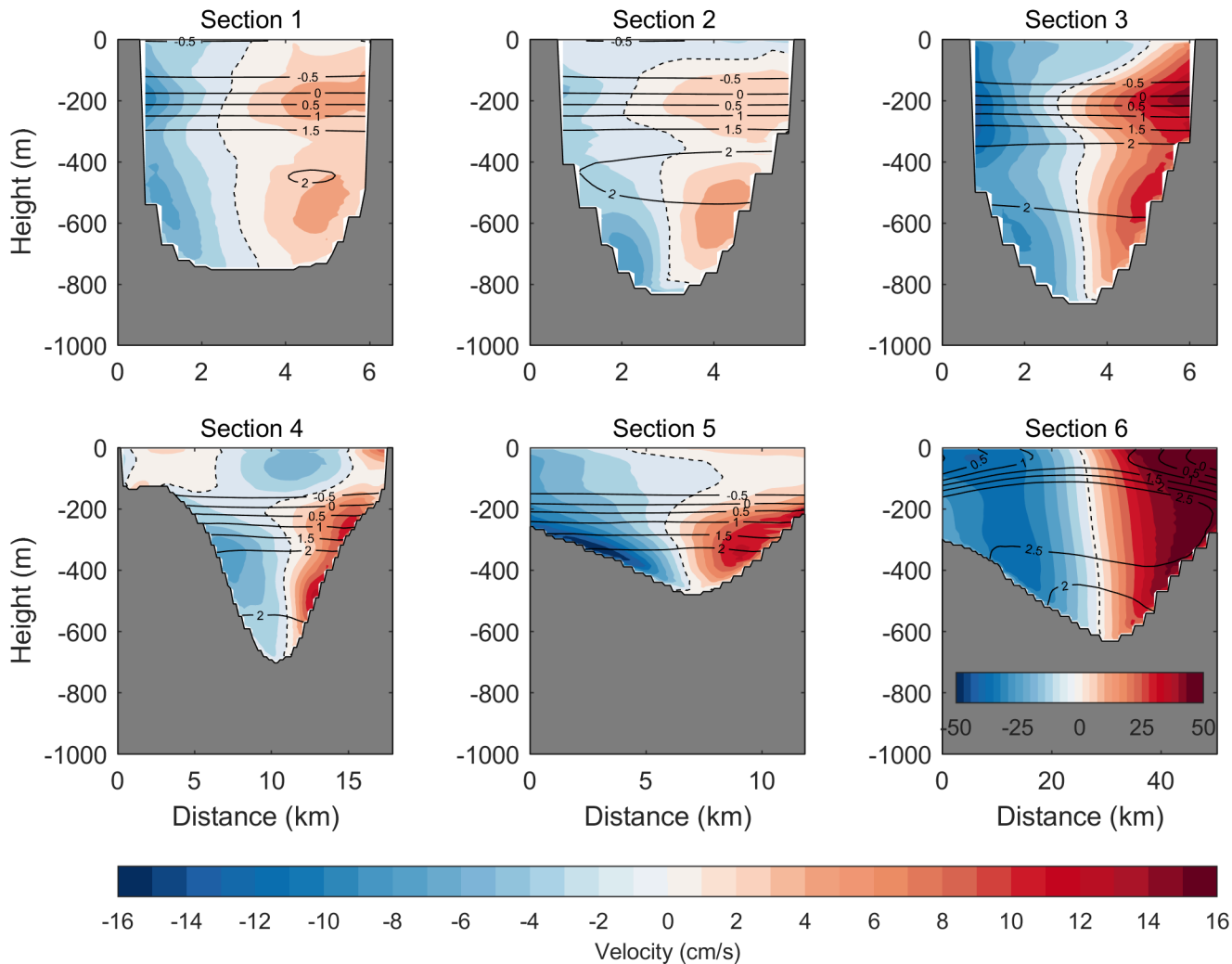


Figure 5.

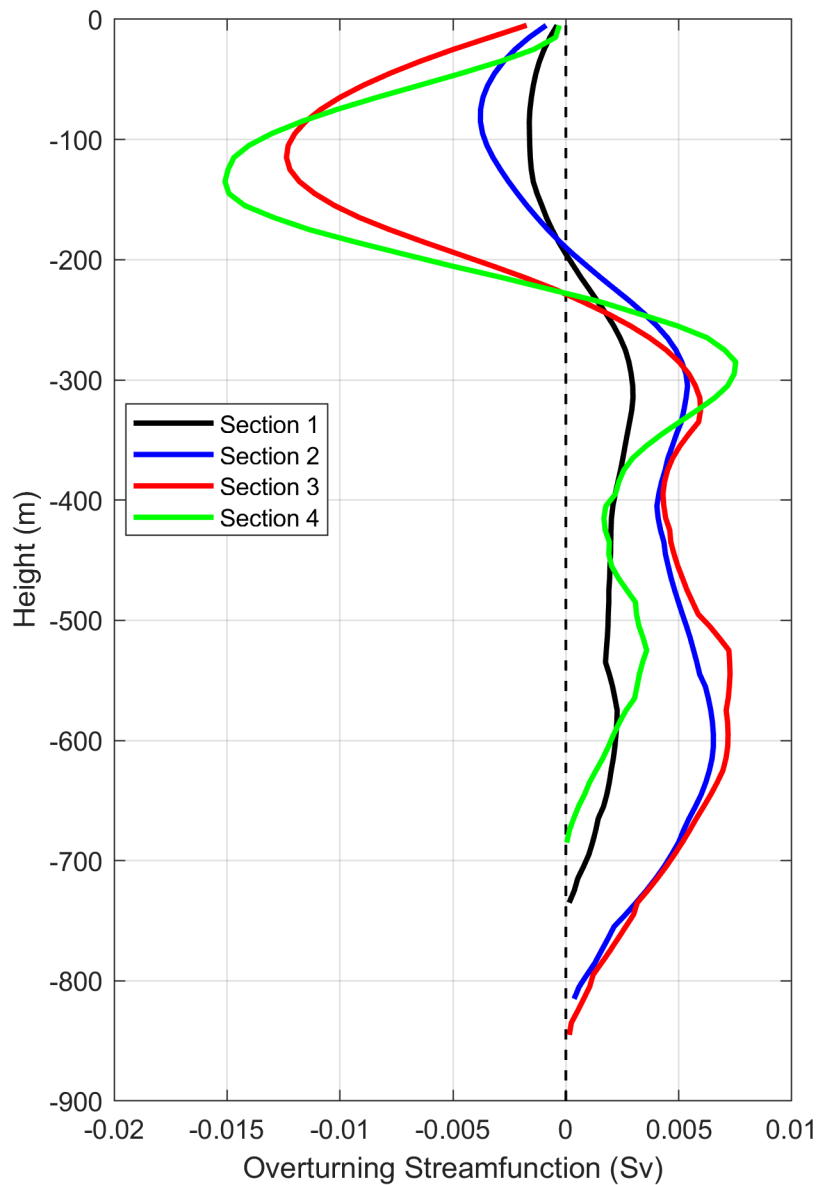


Figure 6.



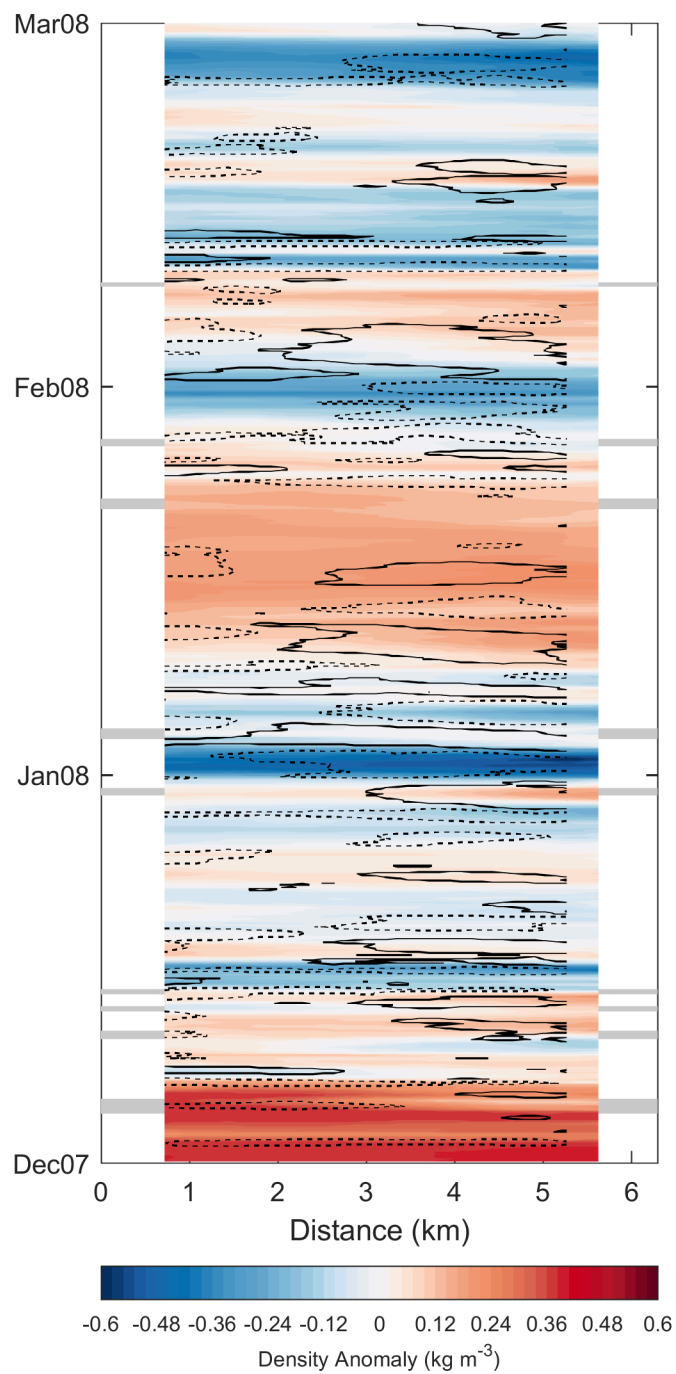
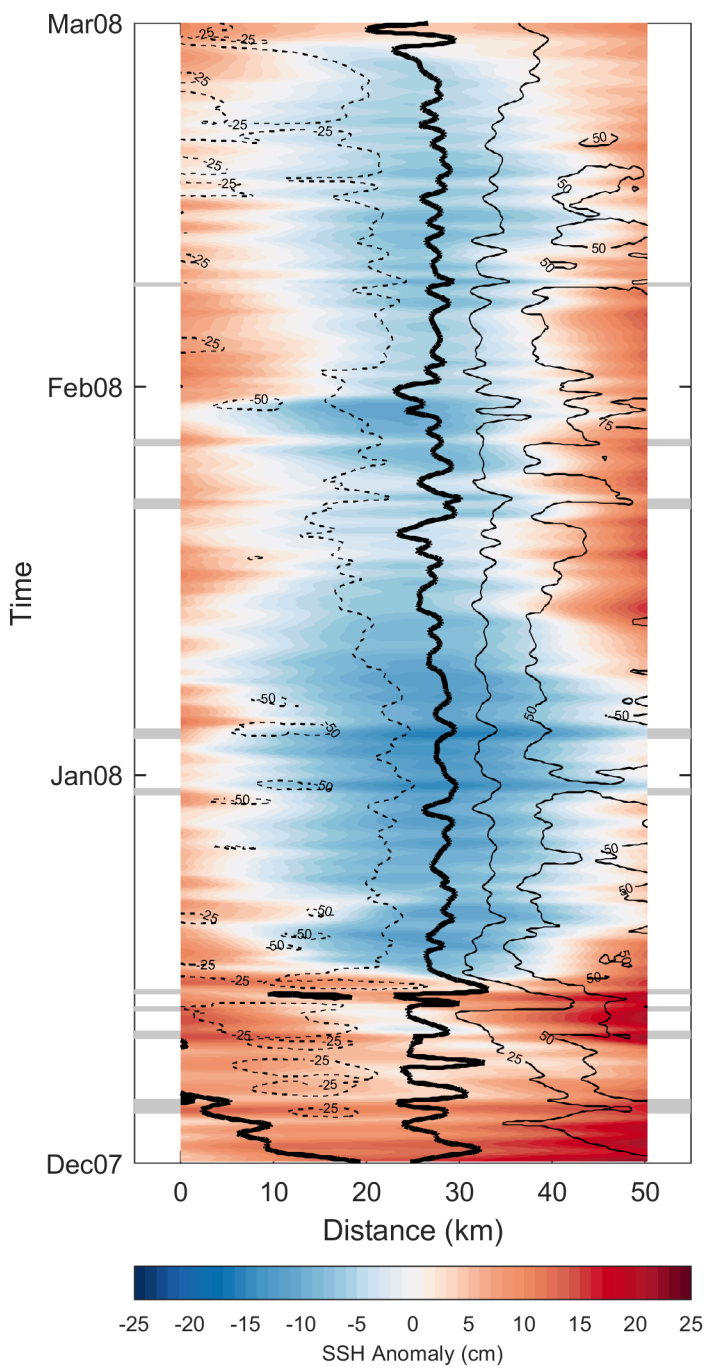
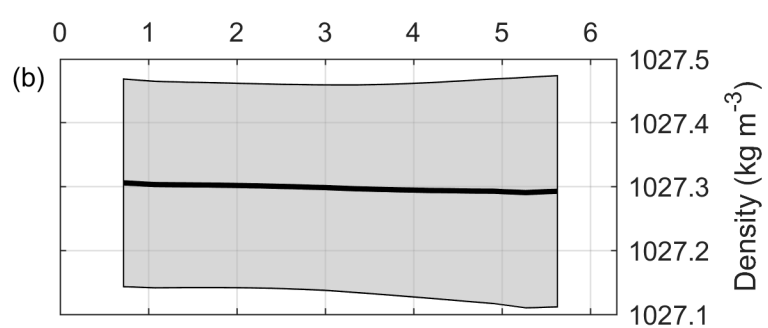
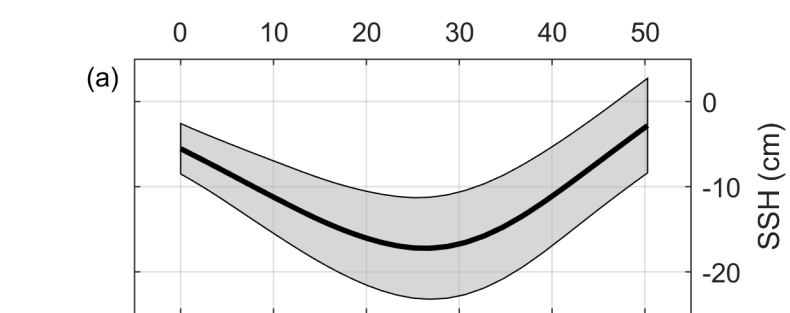
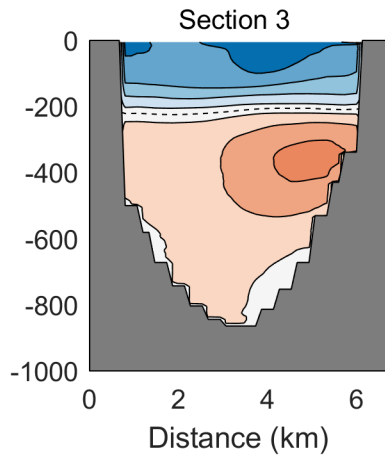
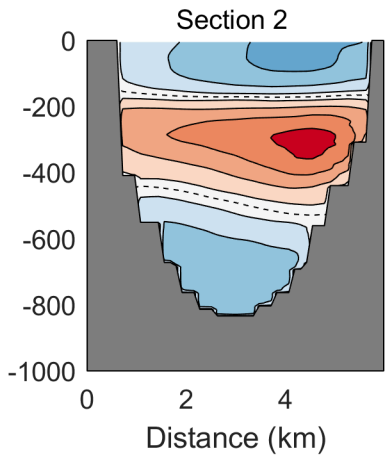
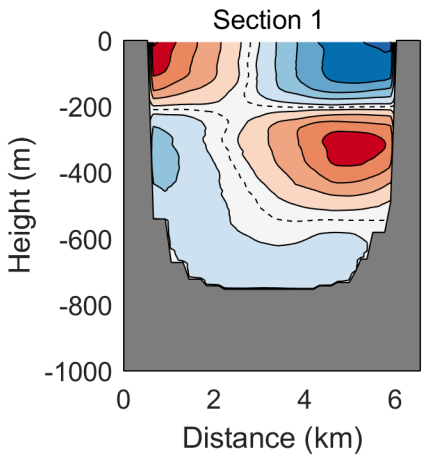
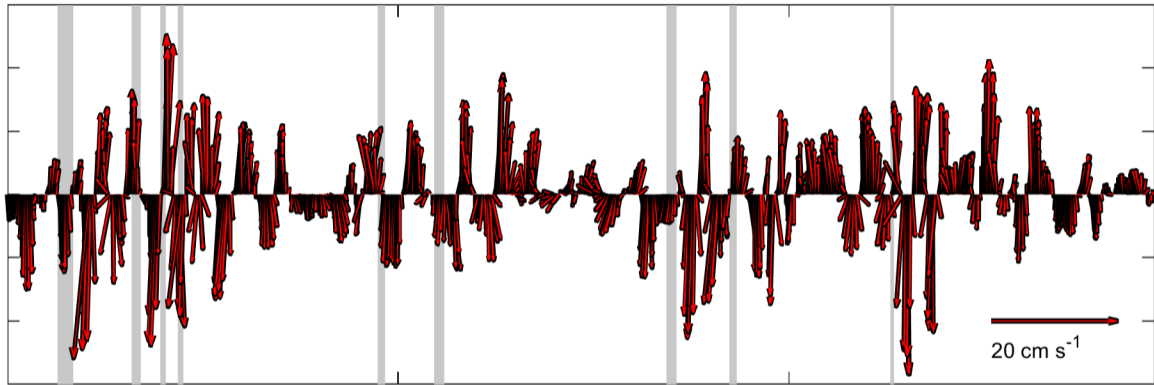


Figure 7.



Amplitude (arbitrary)

Figure 8.



Dec07

Jan08

Feb08

Mar08

Time

Figure 9.



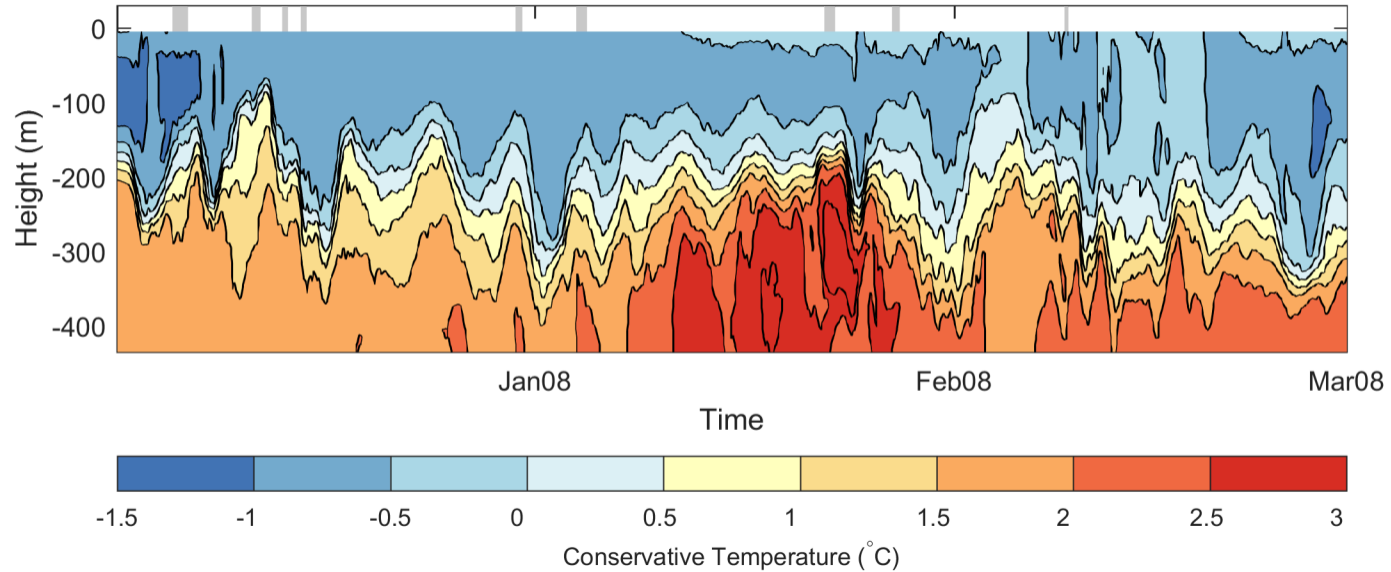


Figure 10.

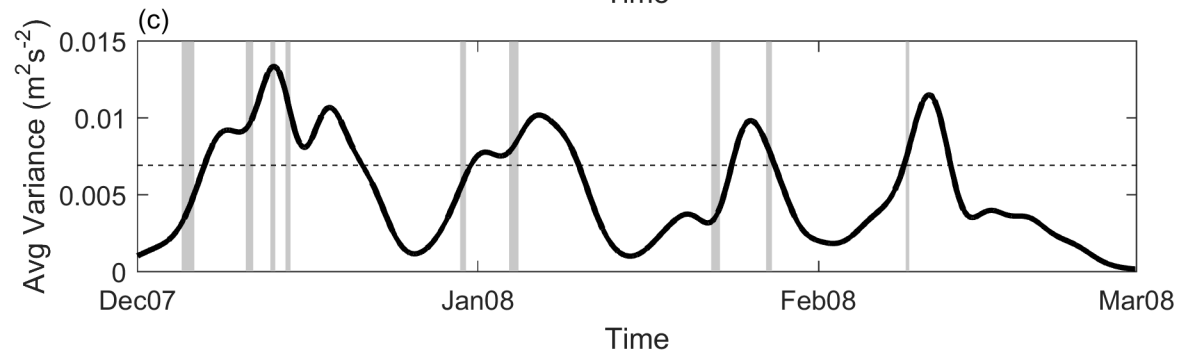
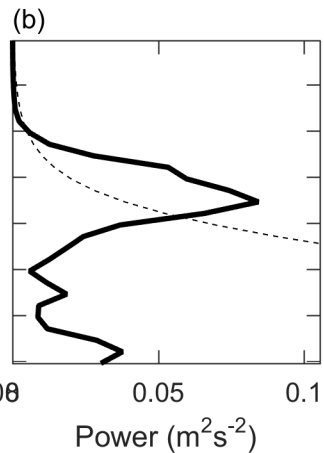
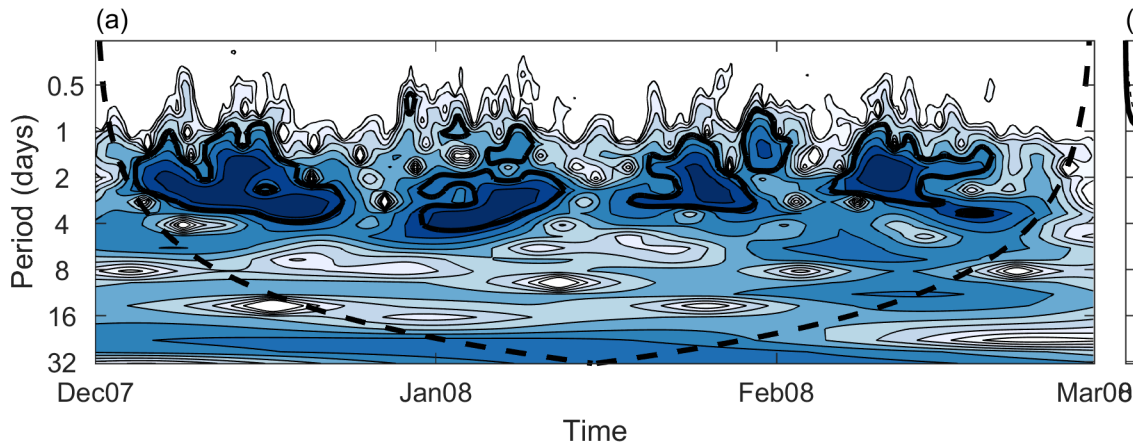


Figure 11.

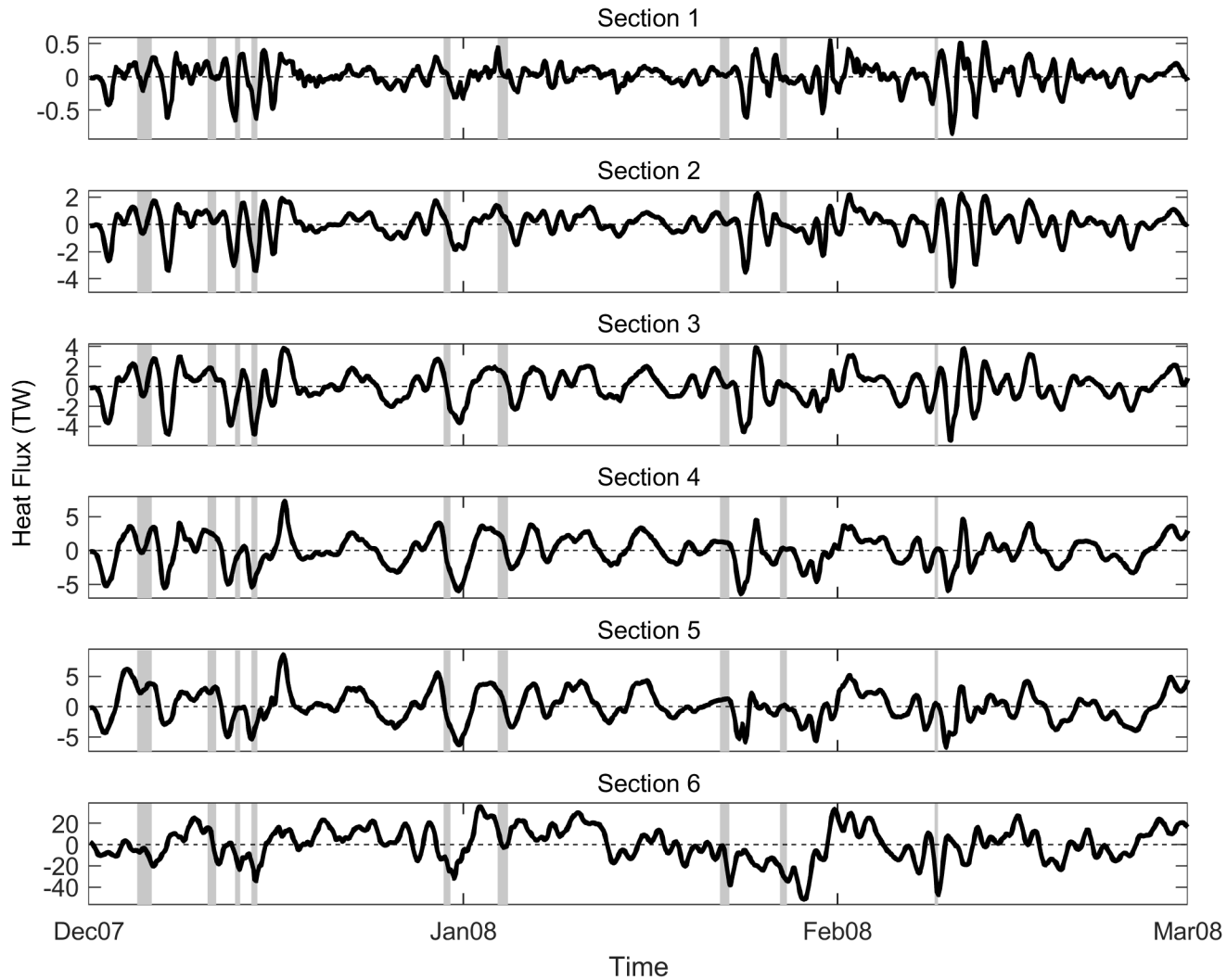


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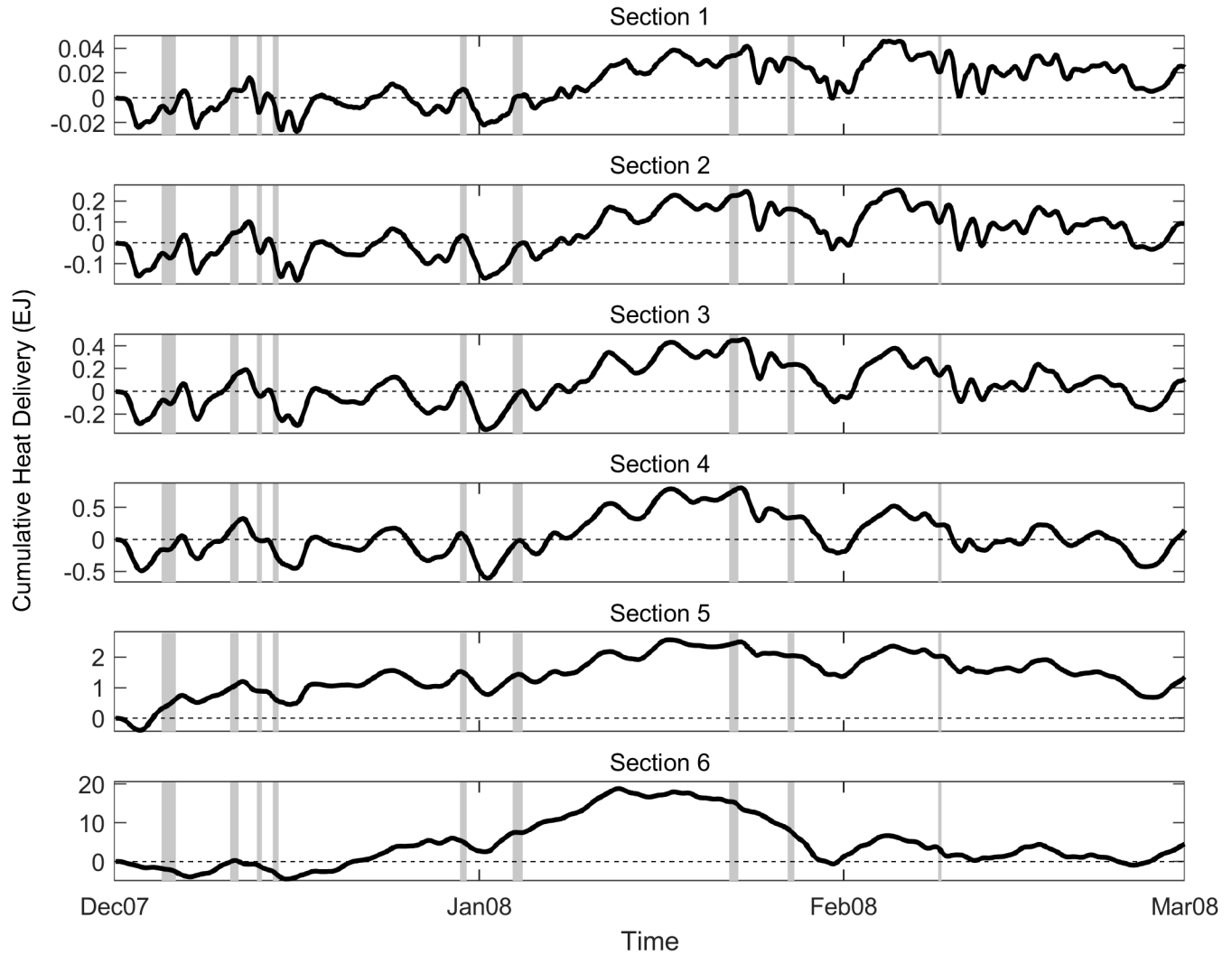


Figure 13.



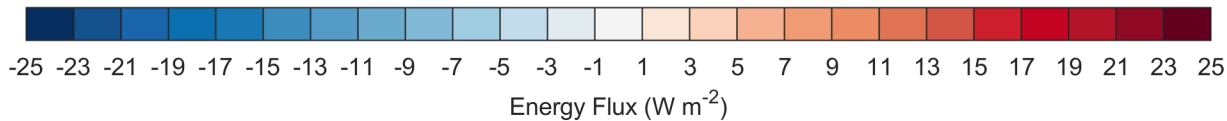
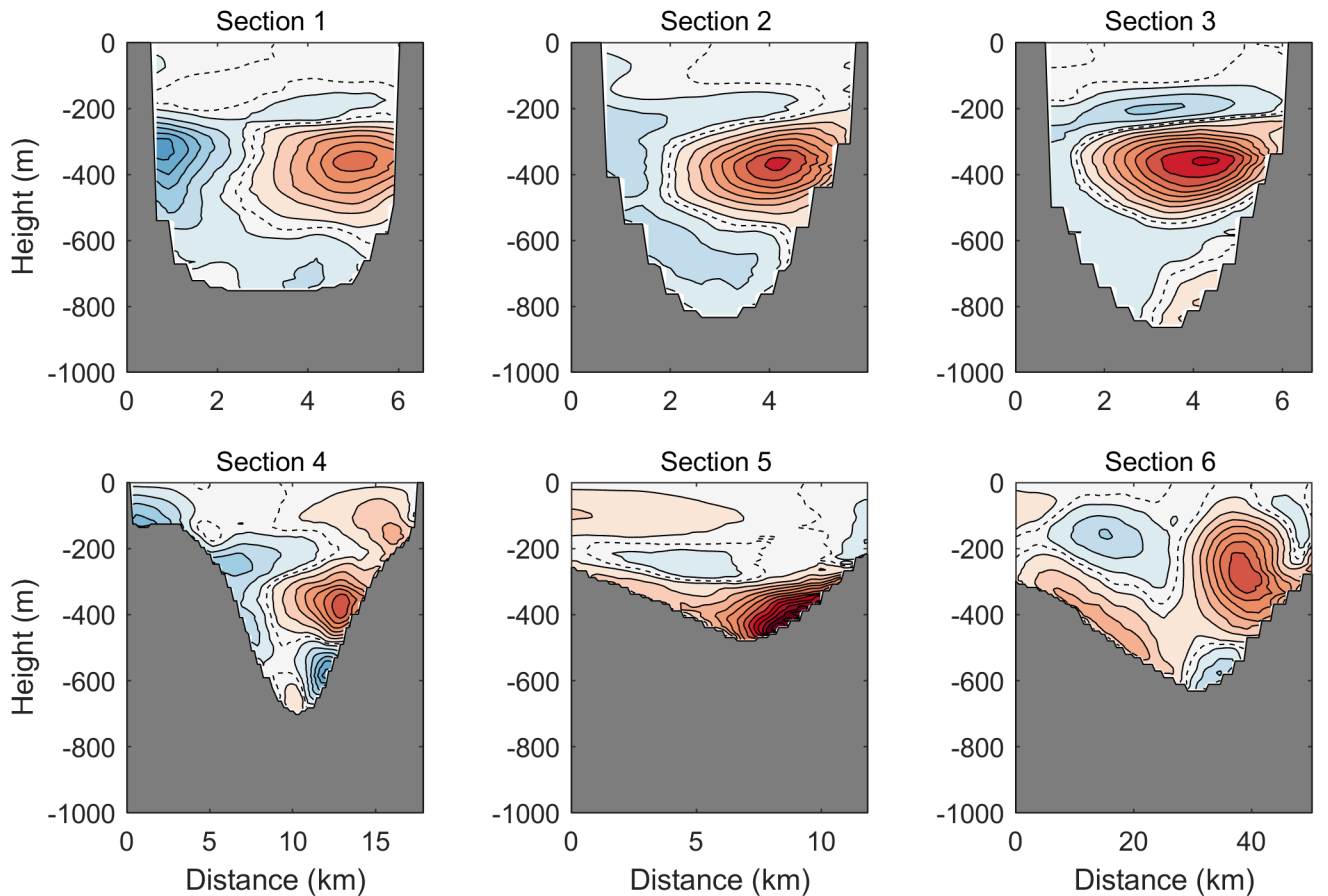


Figure 14.

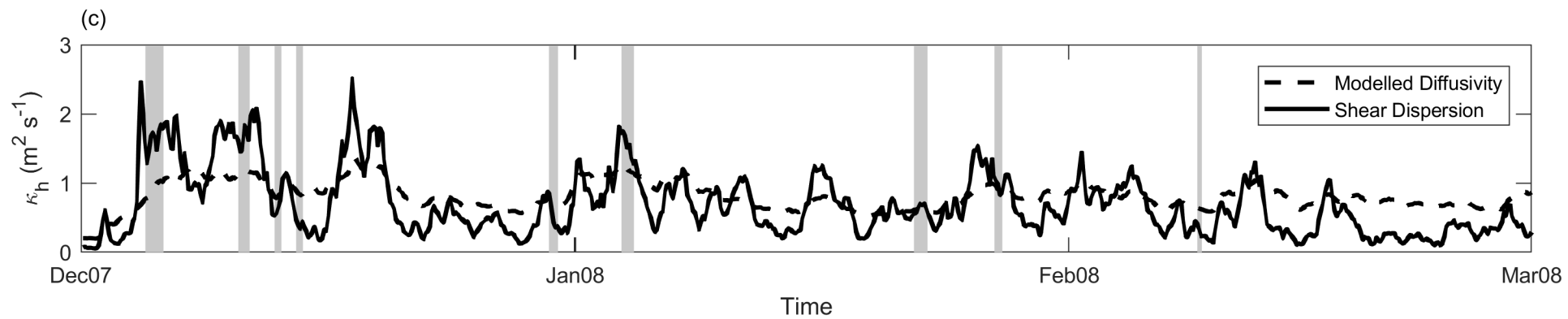
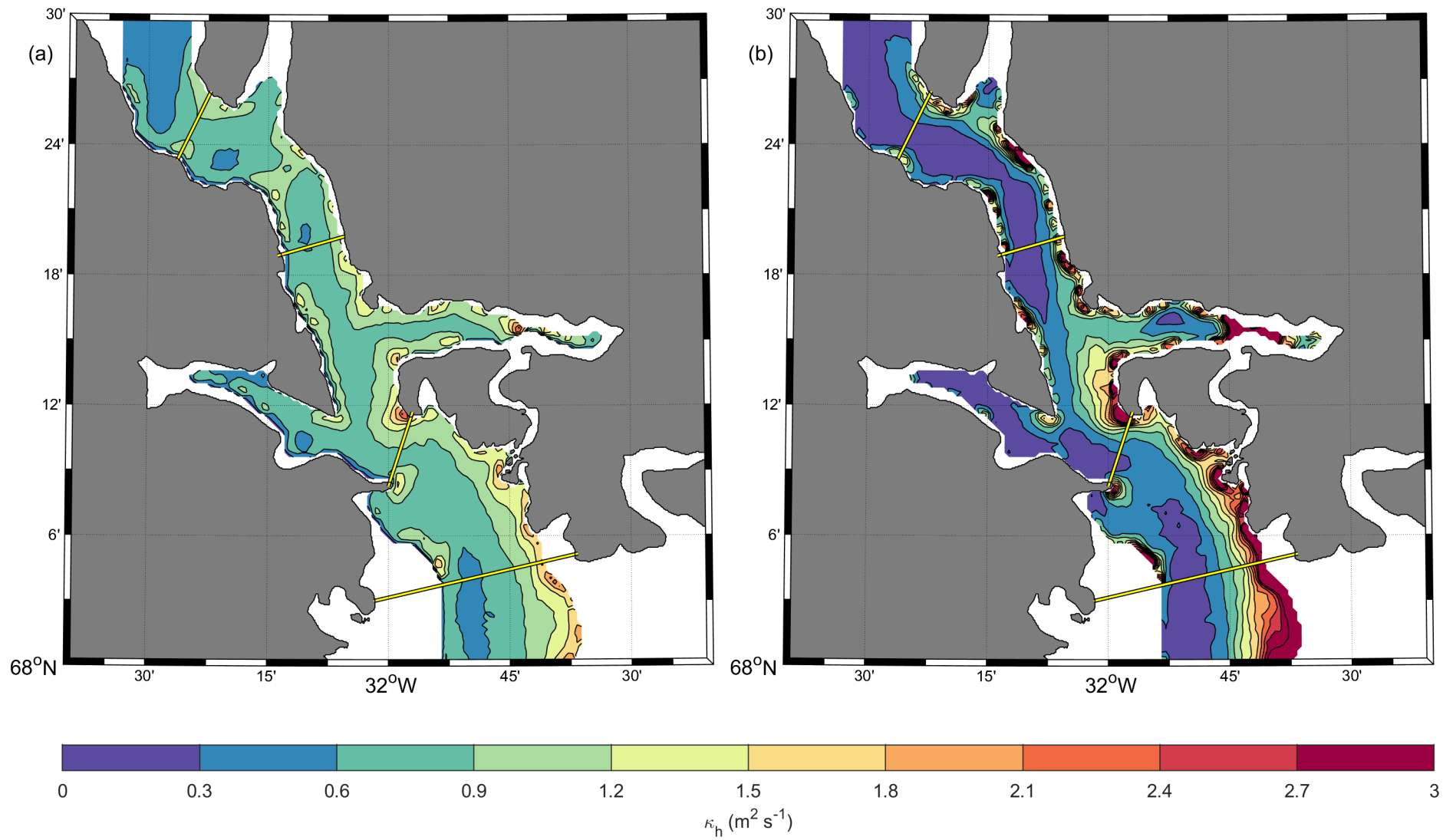
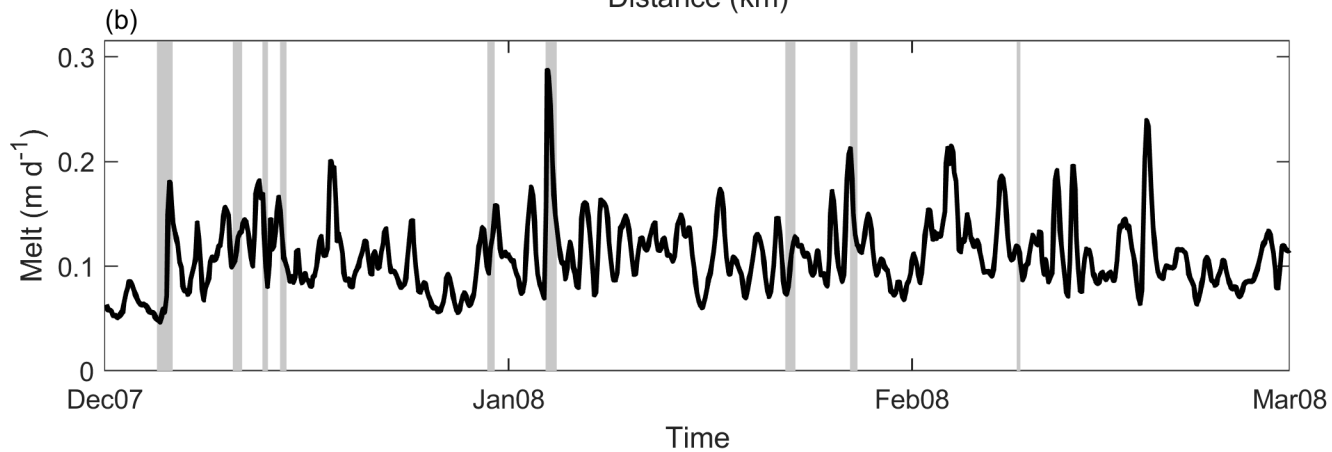
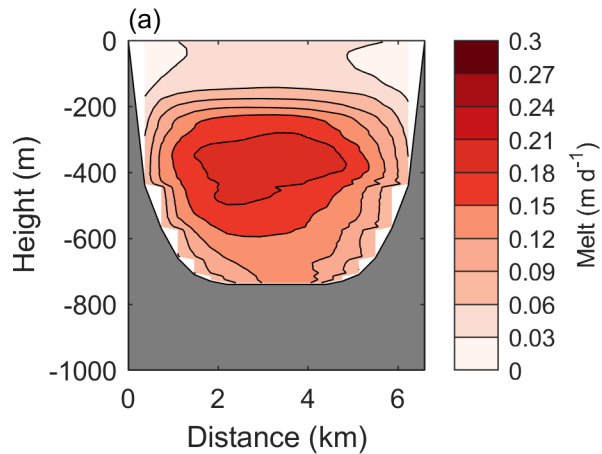


Figure 15.



**Figure 16.**

